

CURSO INTENSIVO

# TERMODINÂMICA E APLICAÇÕES DE ENGENHARIA

## CICLOS DE POTÊNCIA AVANÇADOS – 2/2

Paulo Seleglim Jr.  
Universidade de São Paulo

Attention to  
Filler Words

AVISO IMPORTANTE:

ALGUNS ALUNOS ESTÃO  
RESPONDENDO OS QUIZZES NO QR  
CODE ERRADO...



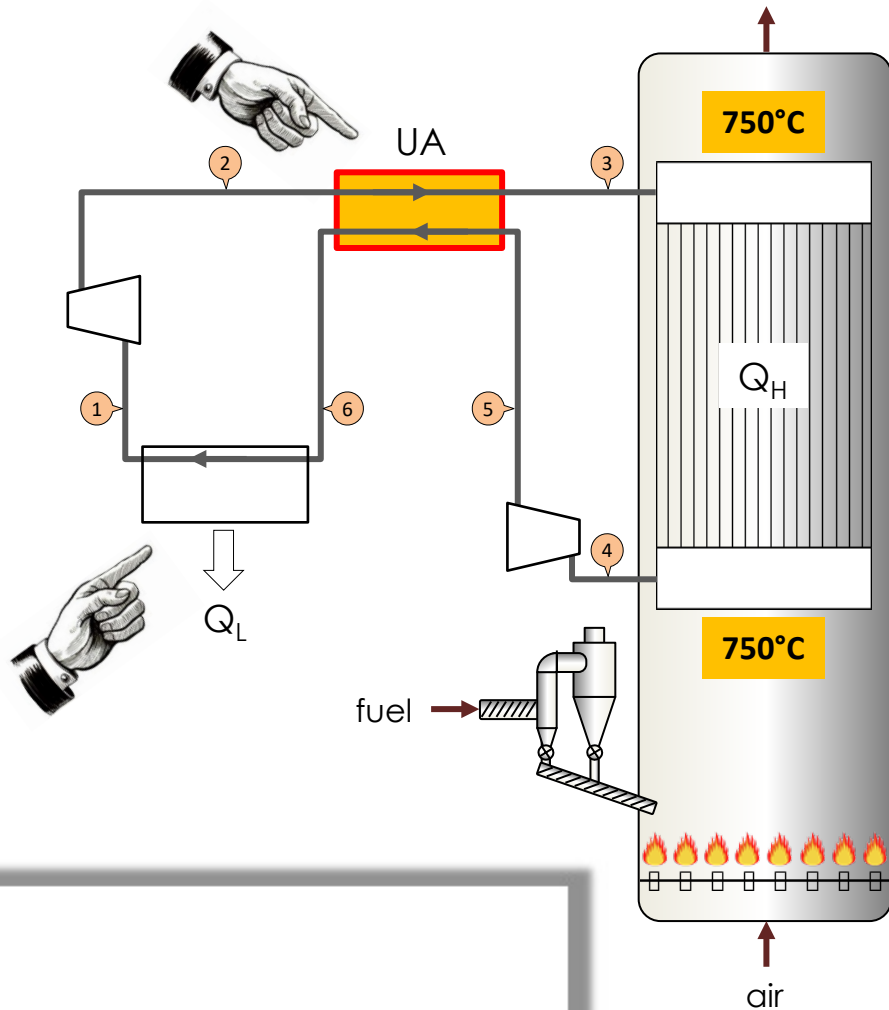
Nesta semana...

Estudo comparativo Rankine, Brayton, Brayton+Rankine @ 750°C / 25°C

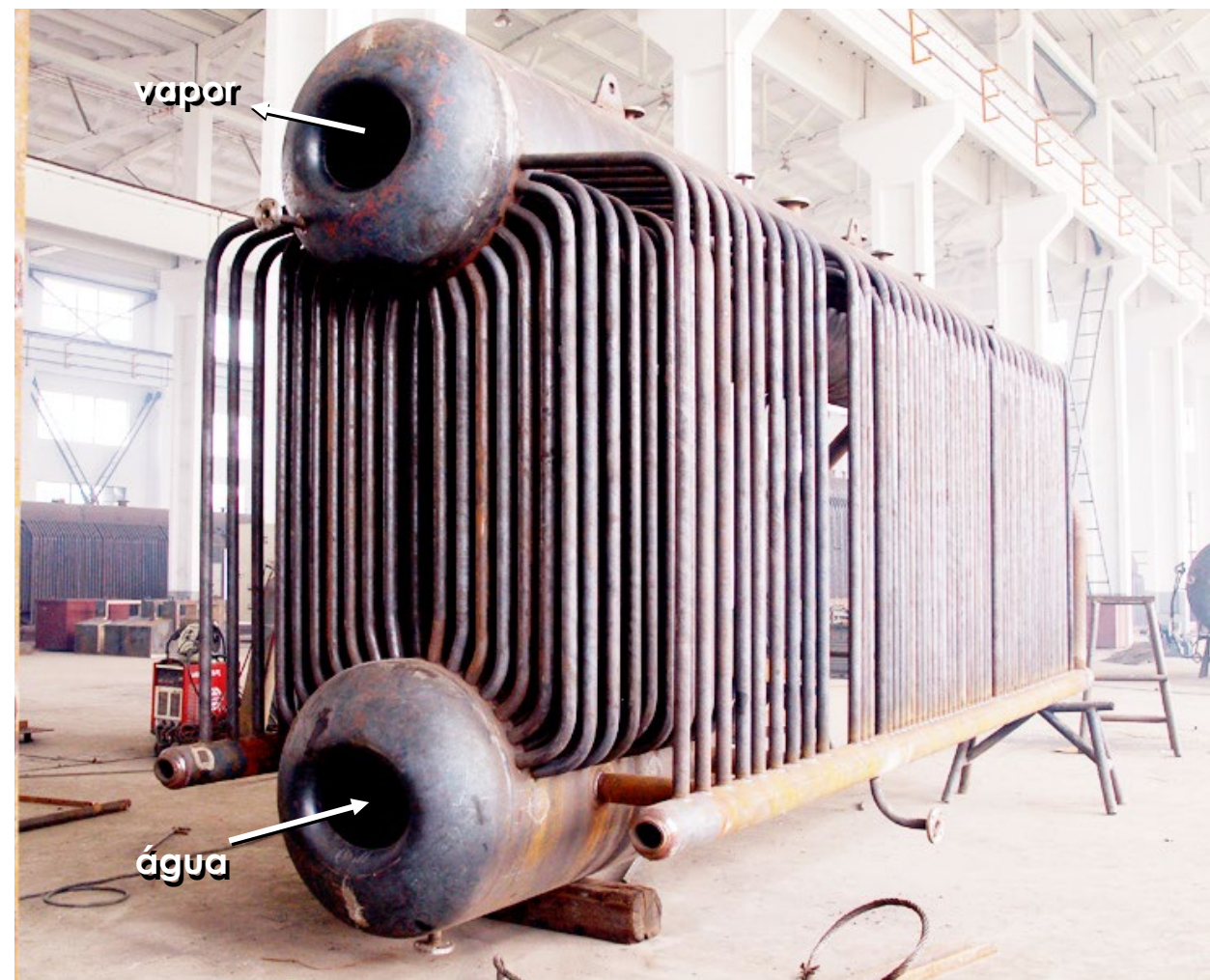
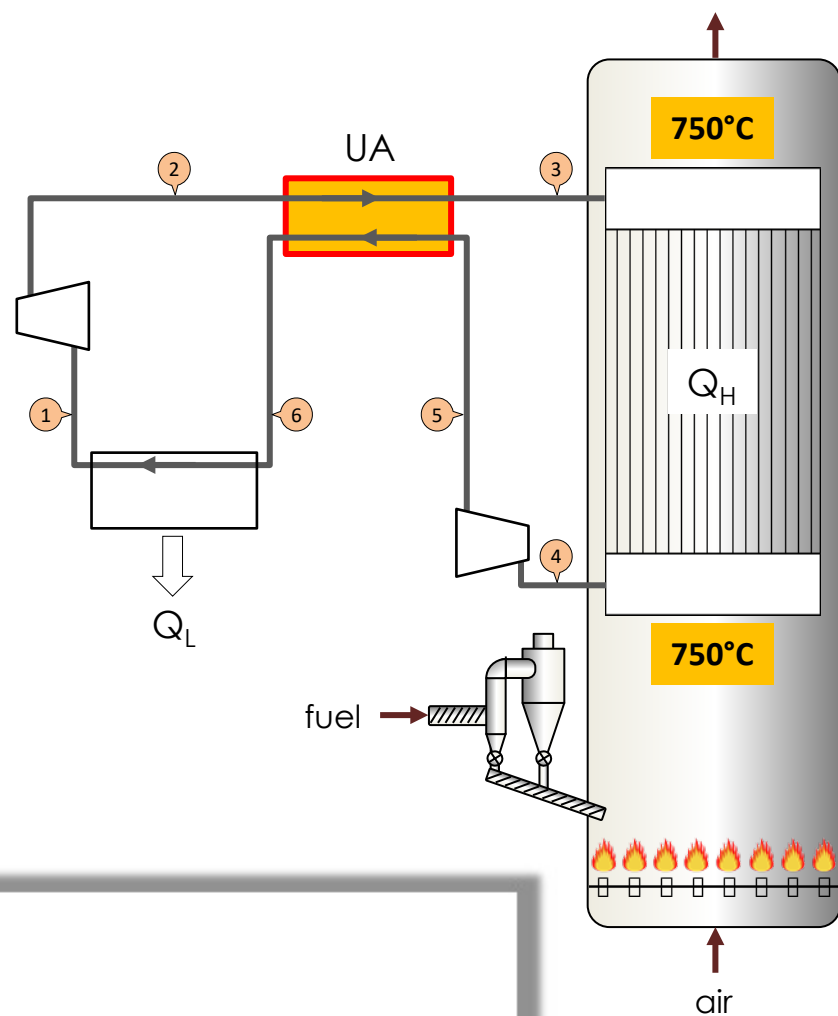
# PARTE 2

Attention to  
Filler Words

# Variação do calor específico com a temperatura e pressão...

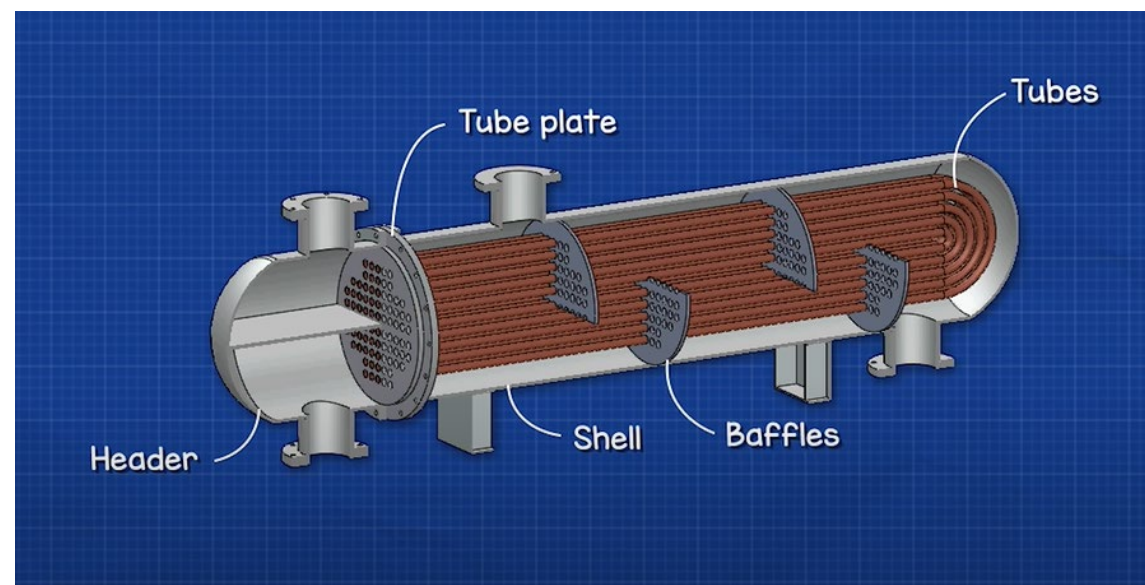
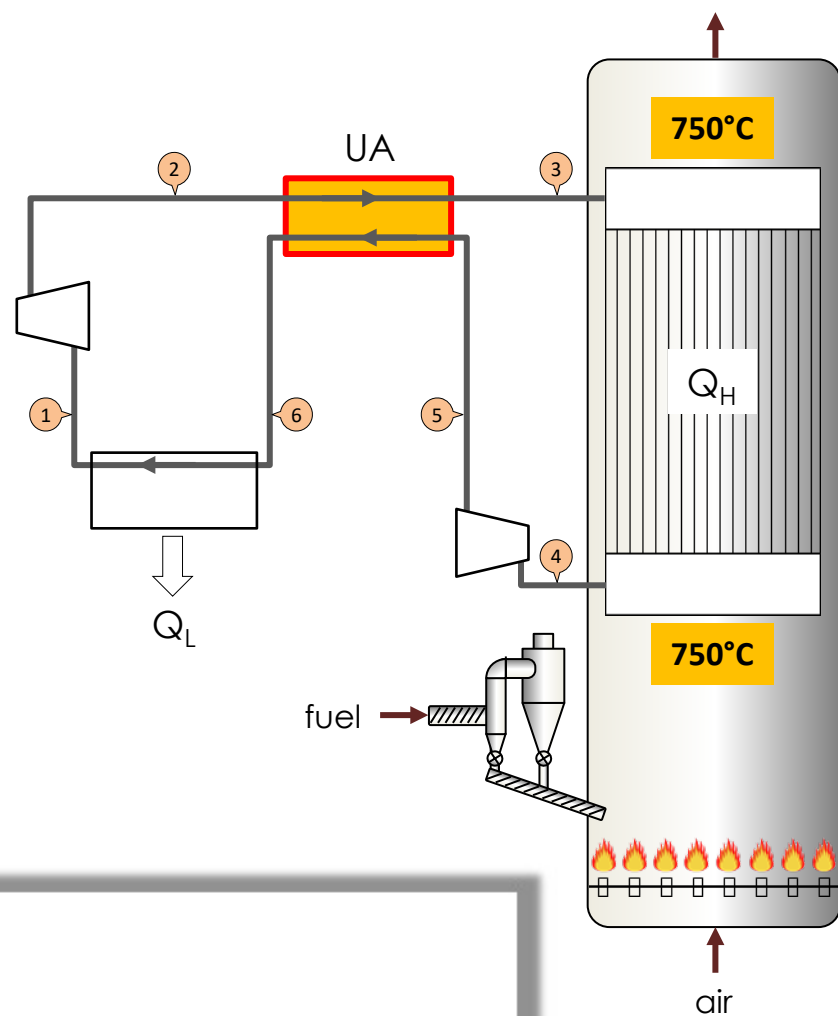


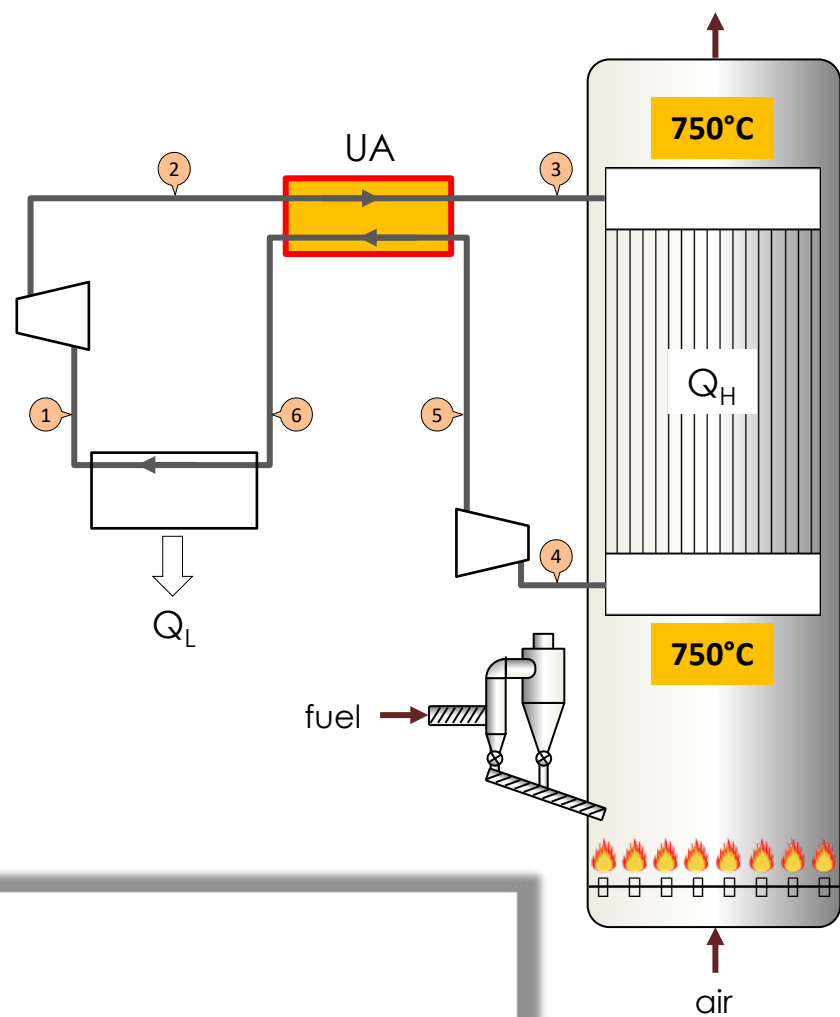
*Modelagem  
dos trocadores de  
calor ???*

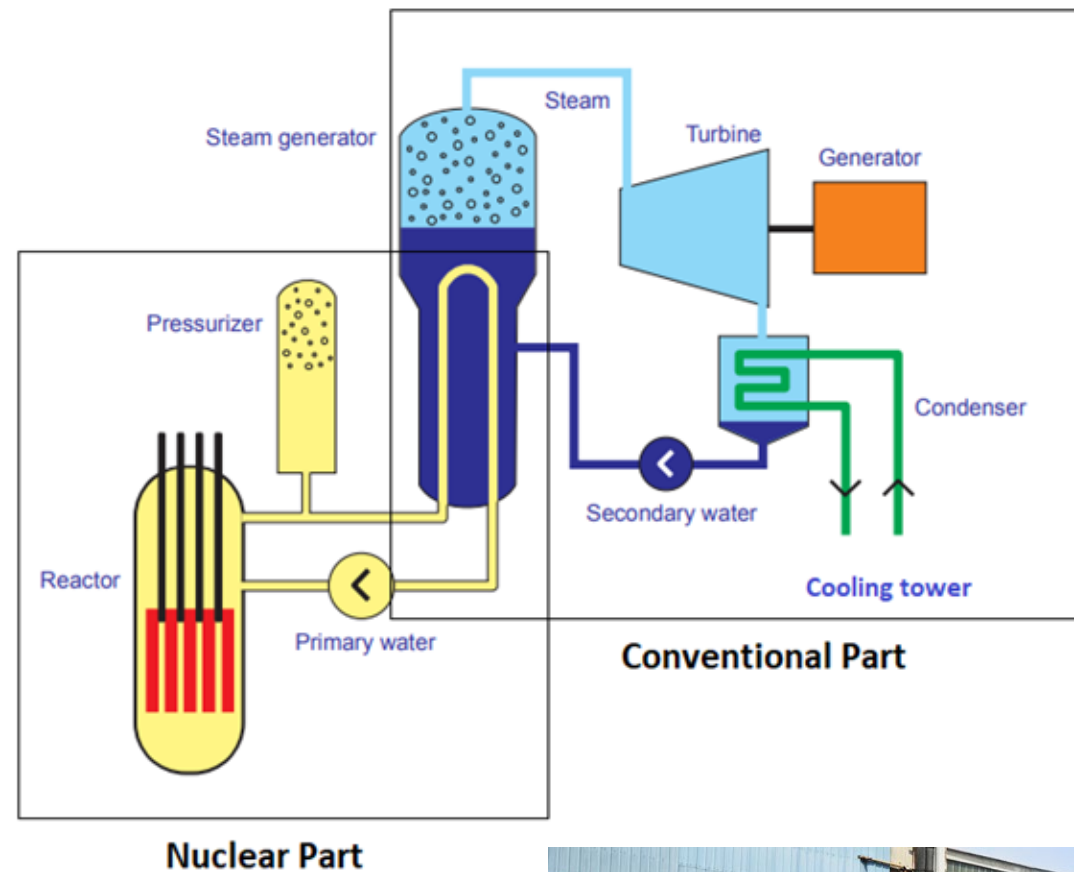
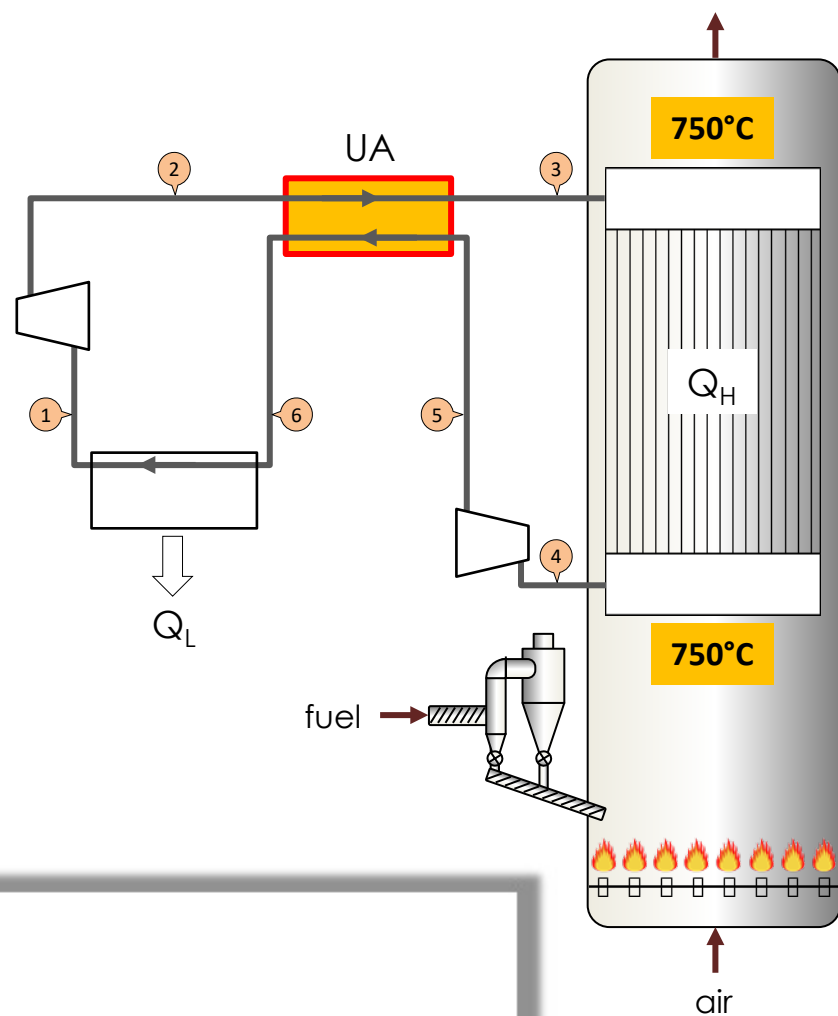


caldeira aquatubular

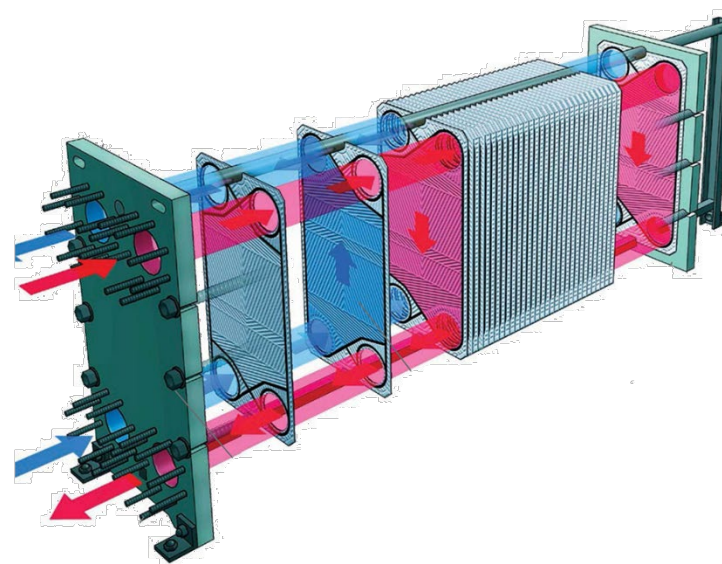
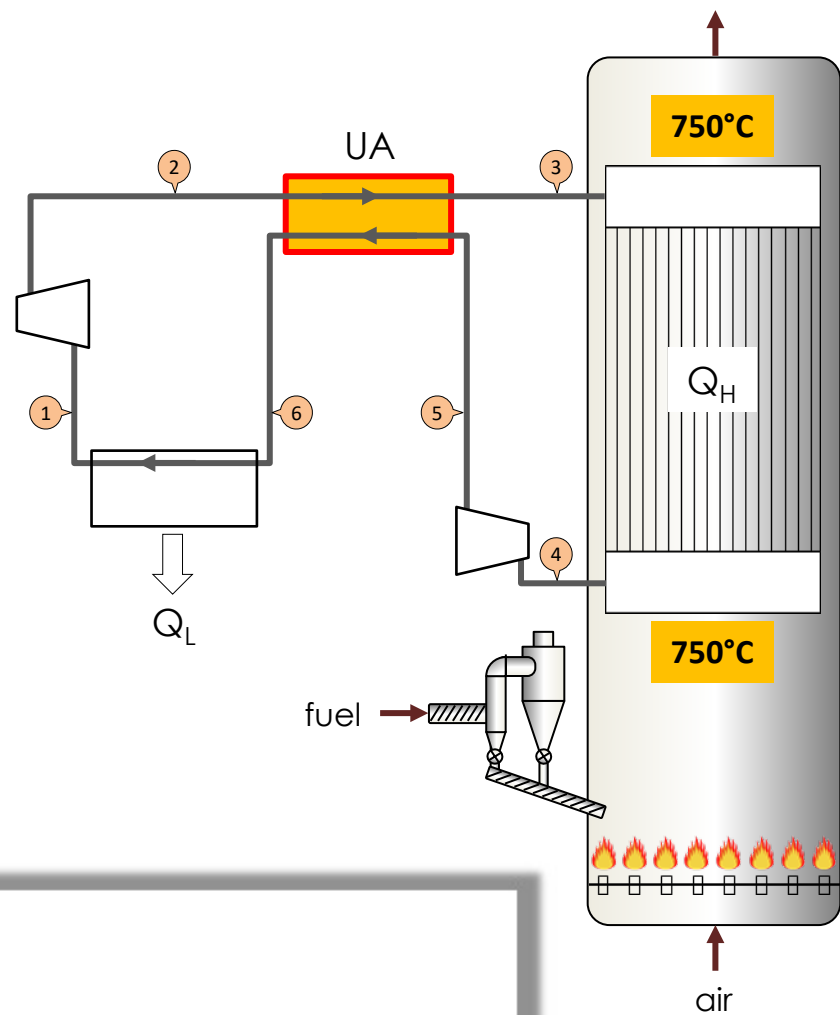


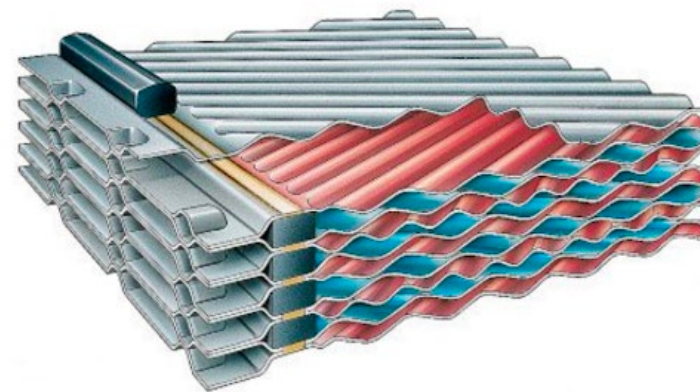
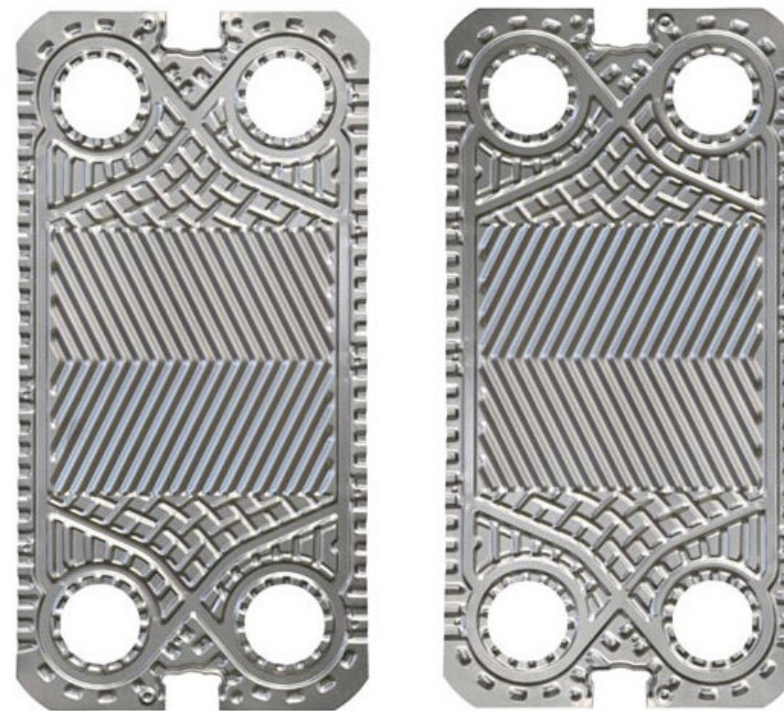
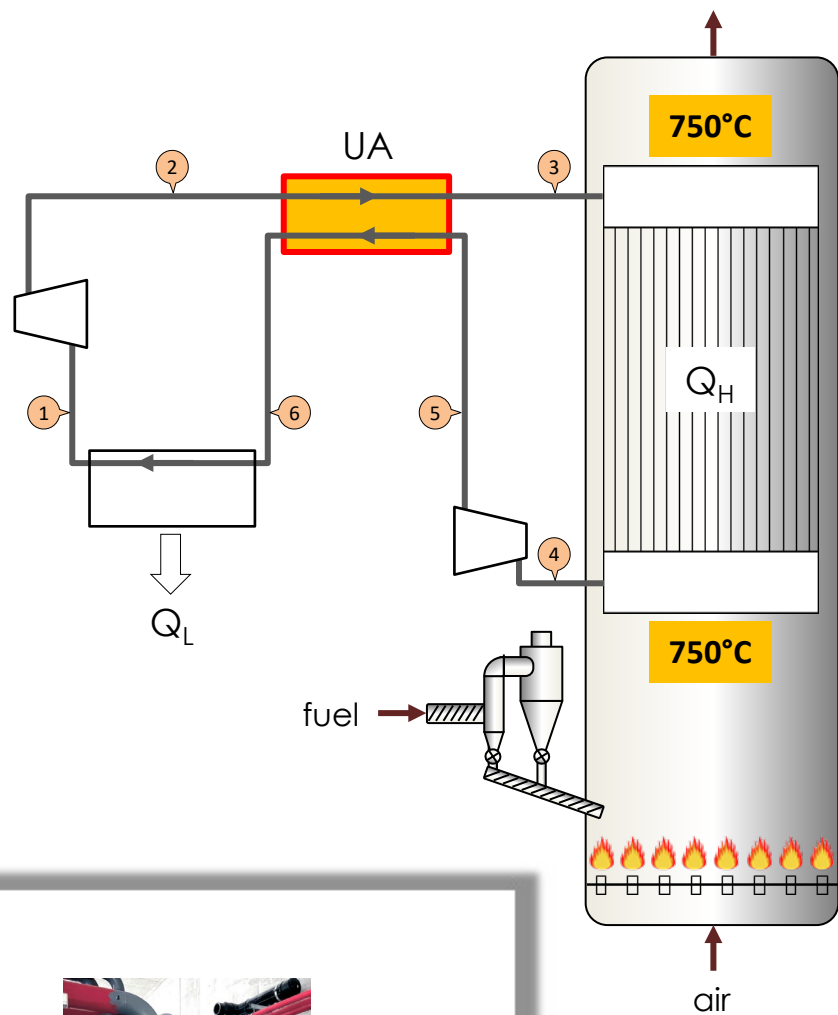








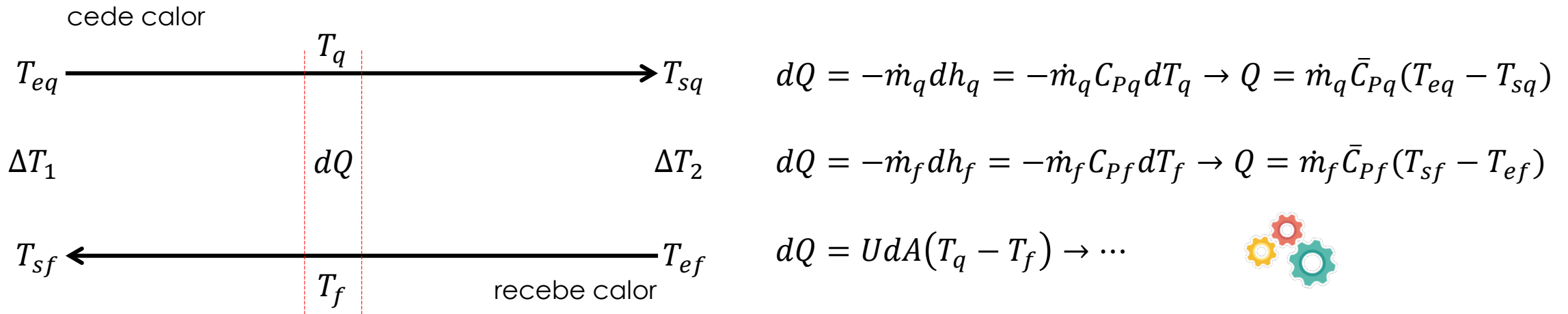






# EQUAÇÕES GOVERNANTES DE UM TROC. E CALOR A CORRENTES PARALELAS

configuração: correntes contrárias ou contracorrentes

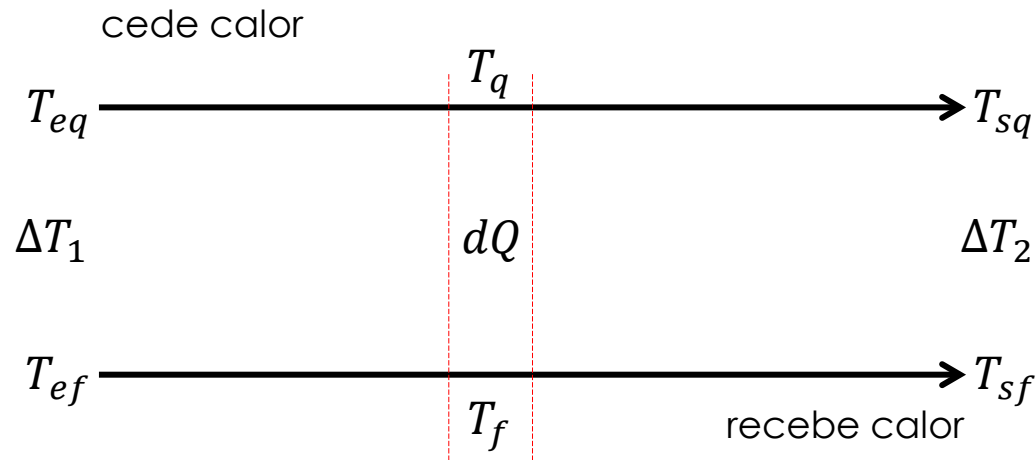


$$\dots Q = UA \frac{(T_{eq} - T_{sf}) - (T_{sq} - T_{ef})}{\ln \left( \frac{T_{eq} - T_{sf}}{T_{sq} - T_{ef}} \right)} = UA \frac{\Delta T_1 - \Delta T_2}{\ln \left( \frac{\Delta T_1}{\Delta T_2} \right)}$$

*Cal. numérico:*  $\rightarrow \Delta T_1 = \Delta T_2 \exp \left( \frac{UA}{Q} (\Delta T_1 - \Delta T_2) \right)$

# EQUAÇÕES GOVERNANTES DE UM TROC. E CALOR A CORRENTES PARALELAS

configuração: concorrentes, paralelas (SIC) ou "cocurrent"



$$dQ = -\dot{m}_q dh_q = -\dot{m}_q C_{Pq} dT_q \rightarrow Q = \dot{m}_q \bar{C}_{Pq} (T_{eq} - T_{sq})$$

$$dQ = +\dot{m}_f dh_f = +\dot{m}_f C_{Pf} dT_f \rightarrow Q = \dot{m}_f \bar{C}_{Pf} (T_{sf} - T_{ef})$$

$$dQ = U dA (T_q - T_f) \rightarrow \dots$$



$$\dots Q = UA \frac{(T_{eq} - T_{ef}) - (T_{sq} - T_{sf})}{\ln \left( \frac{T_{eq} - T_{ef}}{T_{sq} - T_{sf}} \right)} = UA \frac{\Delta T_1 - \Delta T_2}{\ln \left( \frac{\Delta T_1}{\Delta T_2} \right)}$$

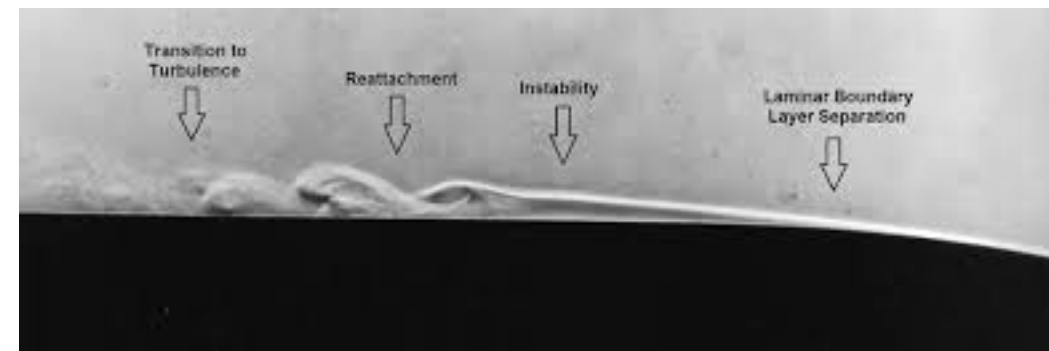
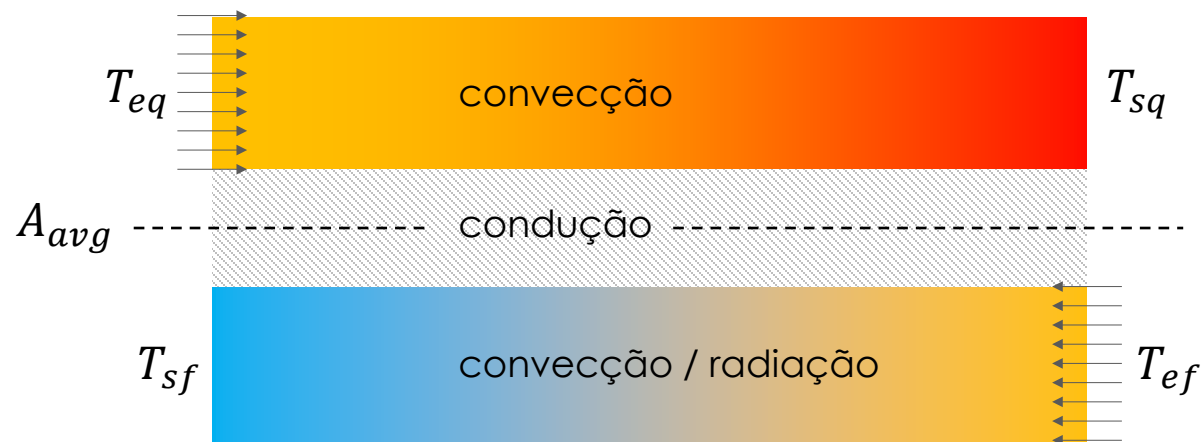


Cal. numérico:  $\rightarrow \Delta T_1 = \Delta T_2 \exp \left( \frac{UA}{Q} (\Delta T_1 - \Delta T_2) \right)$





$$Q = UA \cdot \Delta T_{ln}$$



$$UA = (R_{conv,q} + R_{cond} + R_{conv,f})^{-1} = UA \left( \frac{1}{h_{conv/rad,q}} + \frac{e}{k_{cond}} + \frac{1}{h_{conv,f}} \right)^{-1}$$

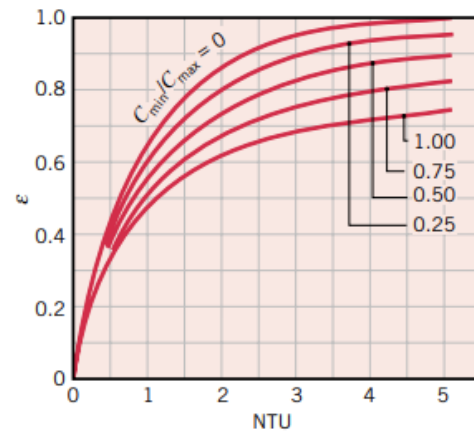
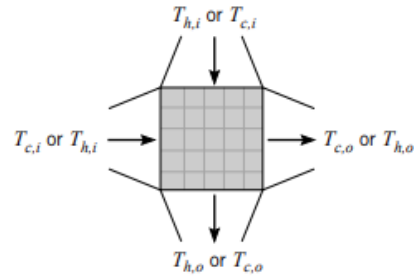
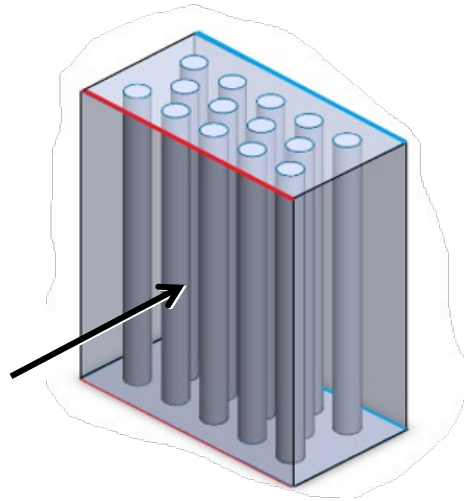
**TABLE 11.2** Representative Values of the Overall Heat Transfer Coefficient

Fluid Combination	$U$ ( $\text{W/m}^2 \cdot \text{K}$ )
Water to water	850–1700
Water to oil	110–350
Steam condenser (water in tubes)	1000–6000
Ammonia condenser (water in tubes)	800–1400
Alcohol condenser (water in tubes)	250–700
Finned-tube heat exchanger (water in tubes, air in cross flow)	25–50

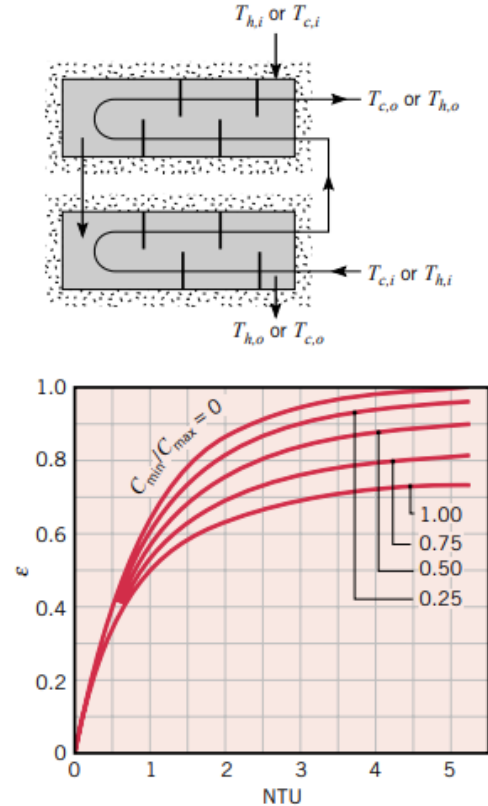
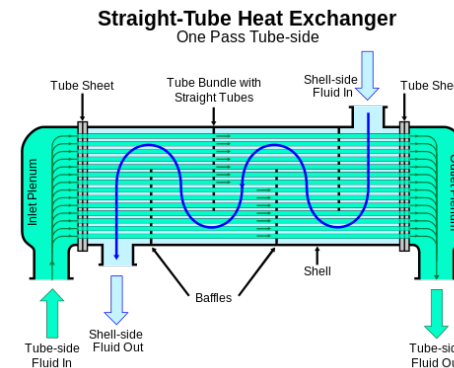


# EQUAÇÕES GOVERNANTES DE UM TROCADOR DE CALOR GENÉRICO

## 1) Método $\varepsilon$ - NUT ("da efetividade")

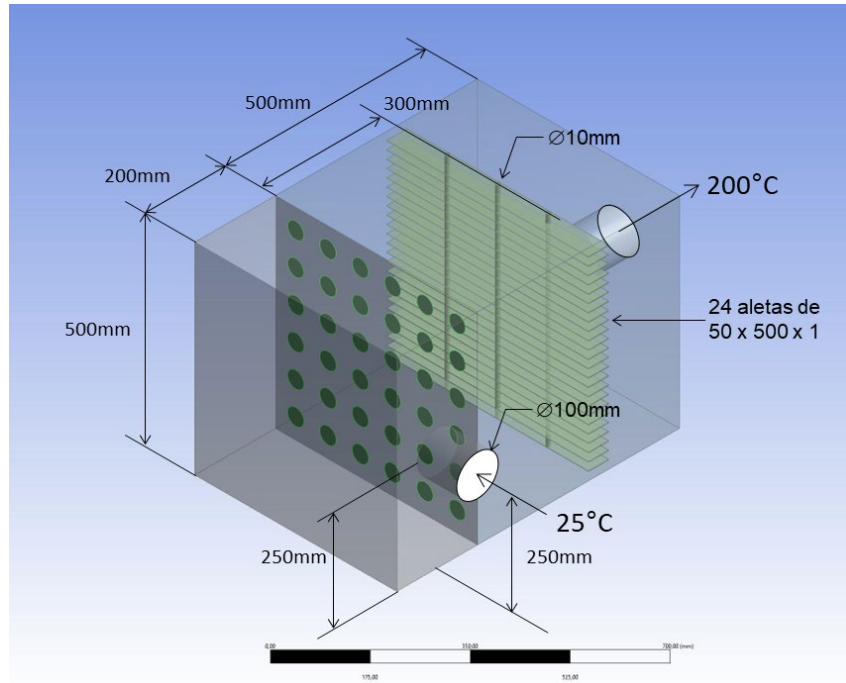


**FIGURE 11.14** Effectiveness of a single-pass, cross-flow heat exchanger with both fluids unmixed (Equation 11.32).

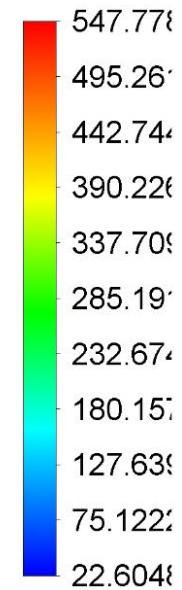


# EQUAÇÕES GOVERNANTES DE UM TROCADOR DE CALOR GENÉRICO

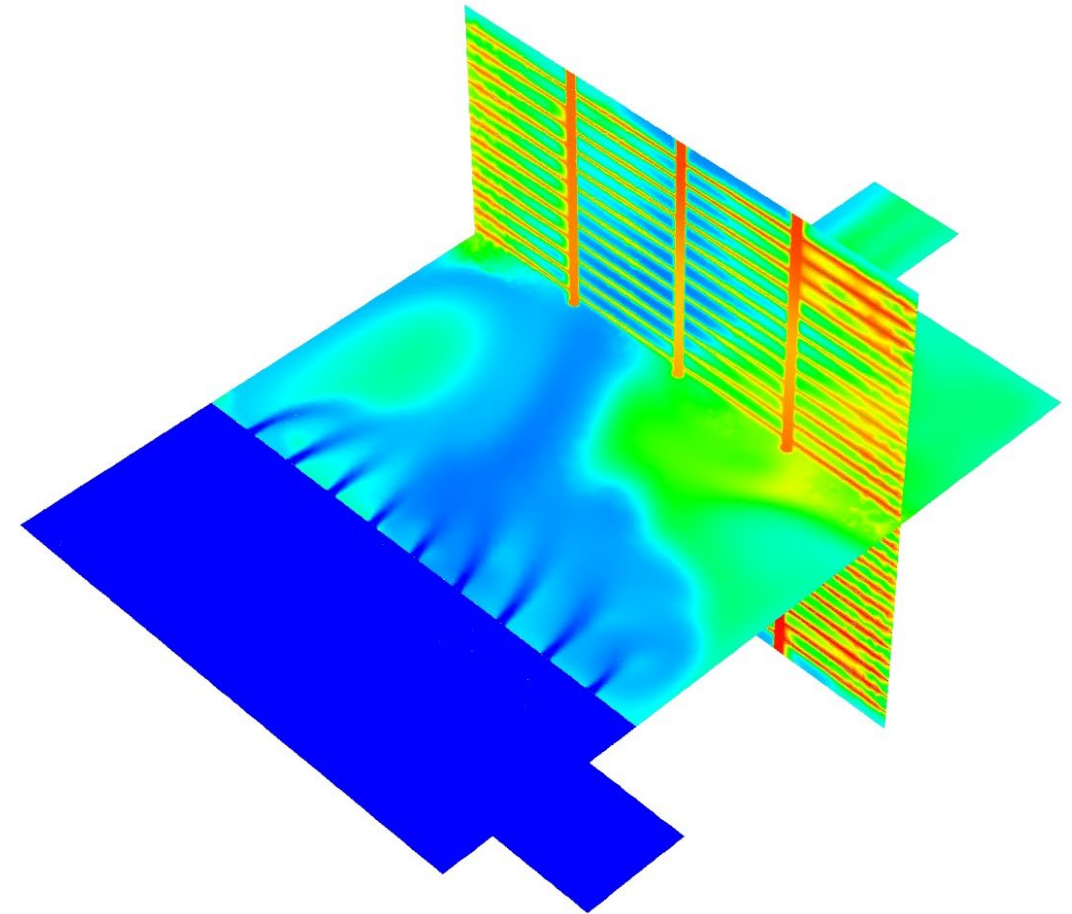
## 2) Método de simulação numérica (CFD)



contour-1  
Static Temperature



[ c ]





Videos - YouTube Studio




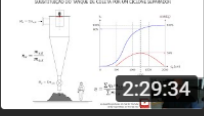
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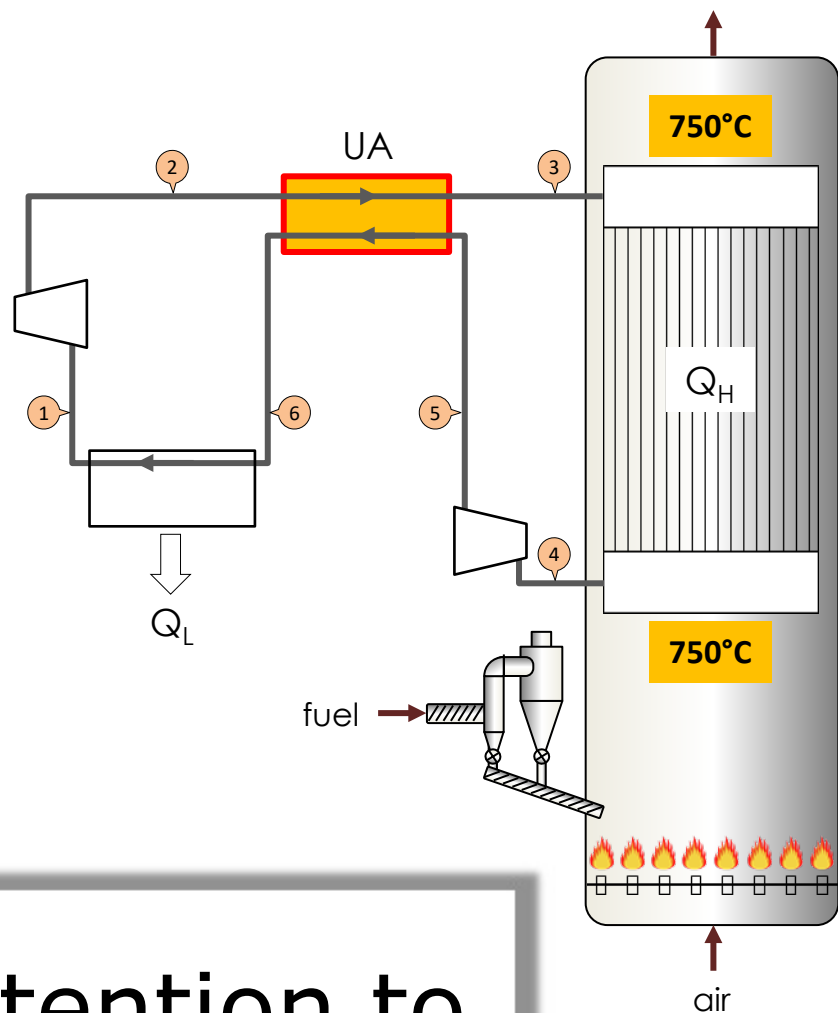
EDIT IN YOUTUBE

Video	Visibility	Monetization	Restrictions	Date
 <div>Aula 1 TUTORIAL CFD ANSYS/FLUEN... Prof. Paulo Seleglim / University of Sao Paulo SEM0551 - Fenômenos de...</div>	Public	Off	None	Sep 11, 2019 Streamed
 <div>TUTORIAL CFD ANSYS/FLUENT: PRO... Prof. Paulo Seleglim / University of Sao Paulo SEM0551 - Fenômenos de...</div>	Public	Off	None	Sep 18, 2019 Streamed
 <div>TUTORIAL CFD ANSYS/FLUENT: PRO... Estarei disponível para tirar dúvidas pelo chat.</div>	Public	Off	None	May 18, 2020 Streamed
 <div>Aula 4 Tutorial: CFD Ansys/Fluent - pr... Prof. Paulo Seleglim / University of Sao Paulo SEM0551 - Fenômenos de...</div>	Public	Off	None	Nov 27, 2019 Streamed

Rows per page: 30 1-4 of many



Análise entrópica do ciclo de potência...



$$Q_R = \dot{m} \cdot (h_3 - h_2)$$

$$Q_R = \dot{m} \cdot (h_5 - h_6)$$

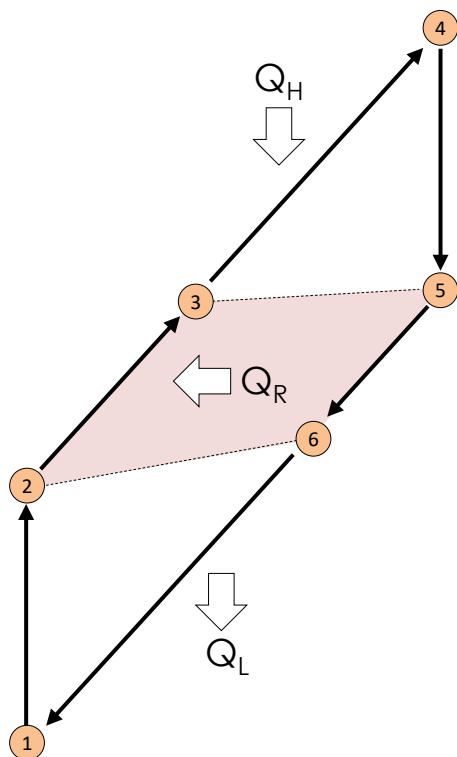
$$Q_R = UA \frac{(T_5 - T_3) - (T_6 - T_2)}{\ln \left( \frac{T_5 - T_3}{T_6 - T_2} \right)}$$

**TABLE 11.2** Representative Values of the Overall Heat Transfer Coefficient

Fluid Combination	$U$ (W/m <sup>2</sup> · K)
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característico...

Attention to  
Filler Words

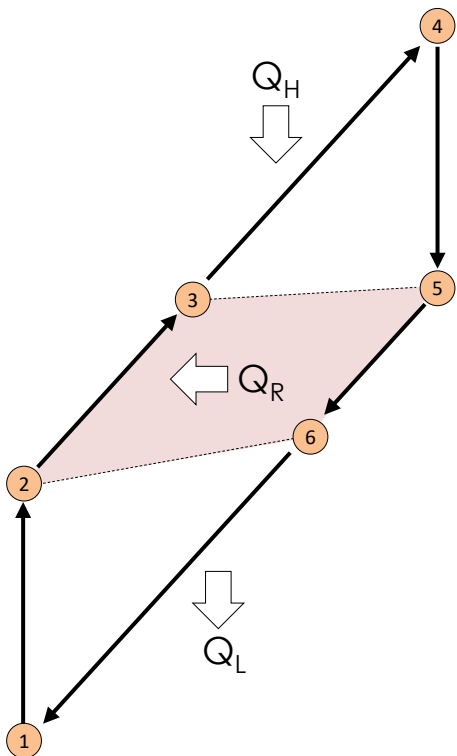


	A	B	C	D	E	F	G	H	I	J	K	L	M	N
1	Fluido	nitrogen												
2	P1	20 bar				xk			fk		QR	T3	T6	
3	T1	25 °C			QR	191,867 kW		f1	0	1	1	-1,1101	0	
4	h1	305,099 kJ/kg			T3	375,389 °C		f2	0	2	1	0	1,06467	
5	s1	5,93705 kJ/kg/K			T6	218,674 °C		f3	0	3	0,02245	0,105	-0,1202	
6														
7	P2	100 bar				xk+1			dxk		QR	T3	T6	
8	T2	201,37 °C			QR	191,867 kW		dQr	0	1	0,4113	0,49107	4,34839	
9	h2	489,46 kJ/kg			T3	375,389 °C		dT3	0	2	-0,5303	0,44236	3,91706	
10	s2	5,93705 kJ/kg/K			T6	218,674 °C		dT6	0	3	-0,3863	0,47802	-4,0843	
11														
12	P4	100 bar												
13	T4	750 °C												
14	h4	1110,11 kJ/kg			h1	305,099 kJ/kg		s1	5,93705 kJ/kg/K		T1	25,00		
15	s4	6,80206 kJ/kg/K			h2	489,46 kJ/kg		s2	5,93705 kJ/kg/K		T2	201,37		
16					h3	681,326 kJ/kg		s3	6,28145 kJ/kg/K		T3	375,39		
17	P5	20 bar			h4	1110,11 kJ/kg		s4	6,80206 kJ/kg/K		T4	750,00		
18	T5	396,591 °C			h5	702,859 kJ/kg		s5	6,80206 kJ/kg/K		T5	396,59		
19	h5	702,859 kJ/kg			h6	510,993 kJ/kg		s6	6,46932 kJ/kg/K		T6	218,67		
20	s5	6,80206 kJ/kg/K												
21					w12	-184,36 kJ/kg		Σenergia	0 kJ/kg					
22	m	1 kg/s			q23	191,867 kJ/kg		rendimento	52,0% kJ/kJ					
23	UA	10 kW/k			q34	428,787 kJ/kg								
24	eps	0,001 -			w45	407,253 kJ/kg		ΣS@rgen	0,01166 kJ/kg/K					
25					q56	-191,87 kJ/kg								
26	macro = ctr + h	solve			q61	-205,89 kJ/kg								

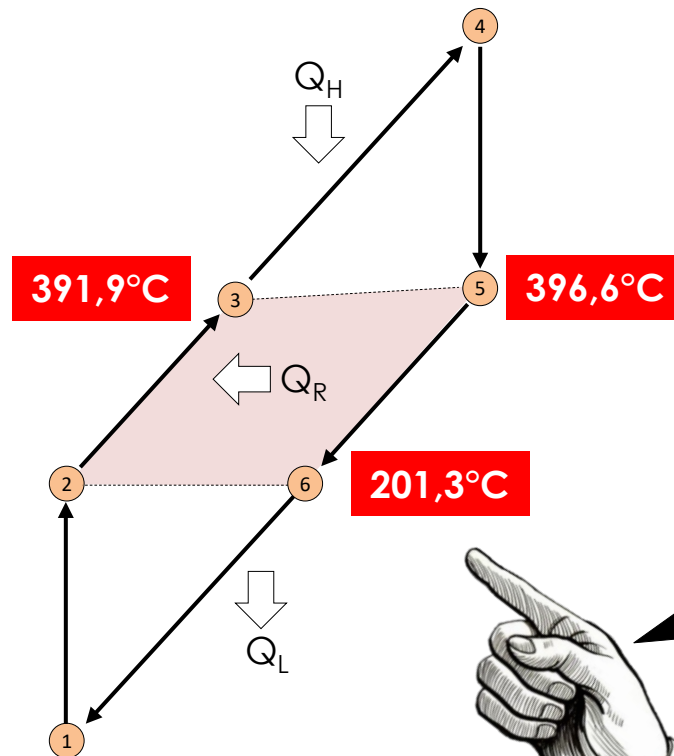
MAXIMIZAÇÃO DA TC (ÁREA) → temperaturas e outras propriedades limite...

BALANÇO ENTRÓPICO → importância relativa das irreversibilidades...





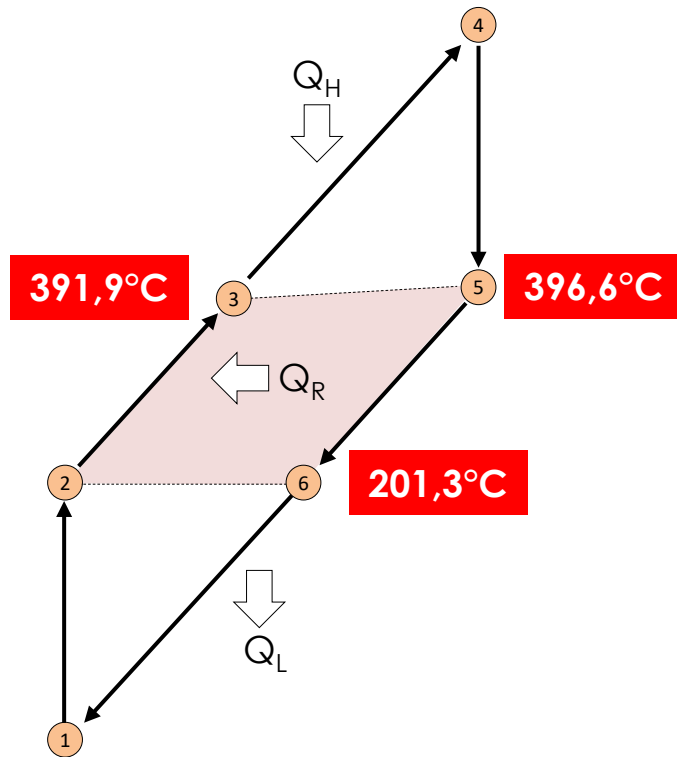
$$UA \rightarrow \infty$$



Tende a  $T_2$  pq  
 $Cp_{56} < Cp_{23}$

Mostrar que com a diminuição de  $UA$ , os delta  $T$ 's aumentam e, conseq., aumenta também a geração de entropia.

$$p/UA \rightarrow \infty$$



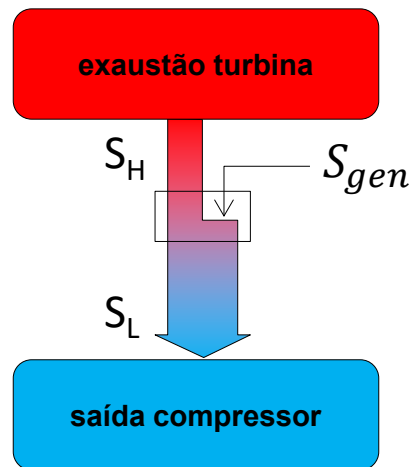
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15	h2	489,46 kJ/kg			h2	489,46	kJ/kg	s2	5,93705	kJ/kg/K		T2	201,37	
16	h3	681,326 kJ/kg			h3	681,326	kJ/kg	s3	6,28145	kJ/kg/K		T3	375,39	
17	h4	1110,11 kJ/kg			h4	1110,11	kJ/kg	s4	6,80206	kJ/kg/K		T4	750,00	
18	h5	702,859 kJ/kg			h5	702,859	kJ/kg	s5	6,80206	kJ/kg/K		T5	396,59	
19	h6	510,993 kJ/kg			h6	510,993	kJ/kg	s6	6,46932	kJ/kg/K		T6	218,67	
20	s5	6,80206 kJ/kg/K												
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25					q56	-191,87	kJ/kg							
26					q61	-205,89	kJ/kg							
27	macro =	ctr + h	solve											

Mostrar que com a diminuição de UA, os delta T's aumentam e, conseq., aumenta também a geração de entropia.

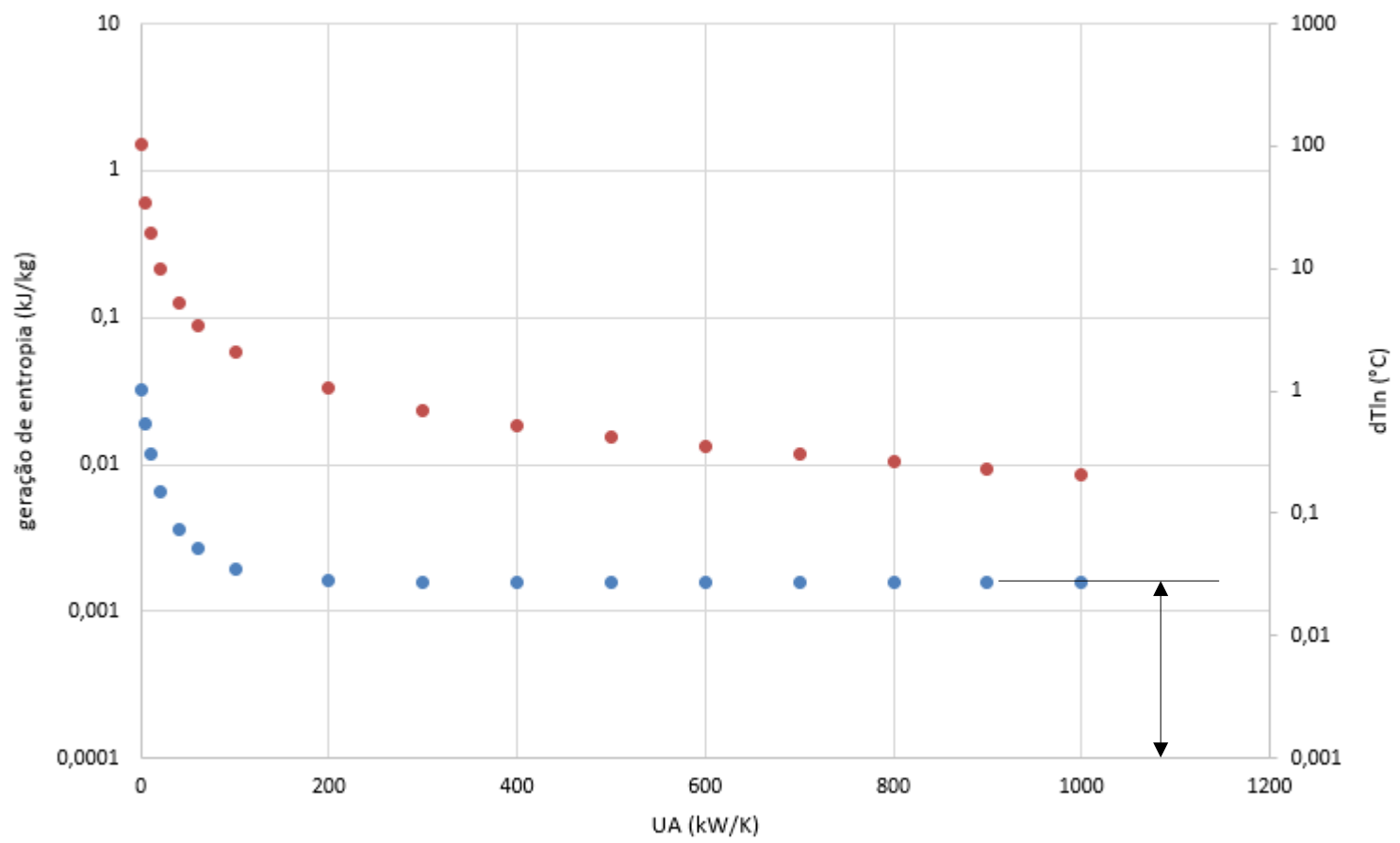
$$\Sigma q - \Sigma w = \dots = 0$$

$$s_{gen} = s_3 - s_2 + s_6 - s_5 = 0,01166 \text{ kJ/kg/K}$$





$S_{gen,\infty}$





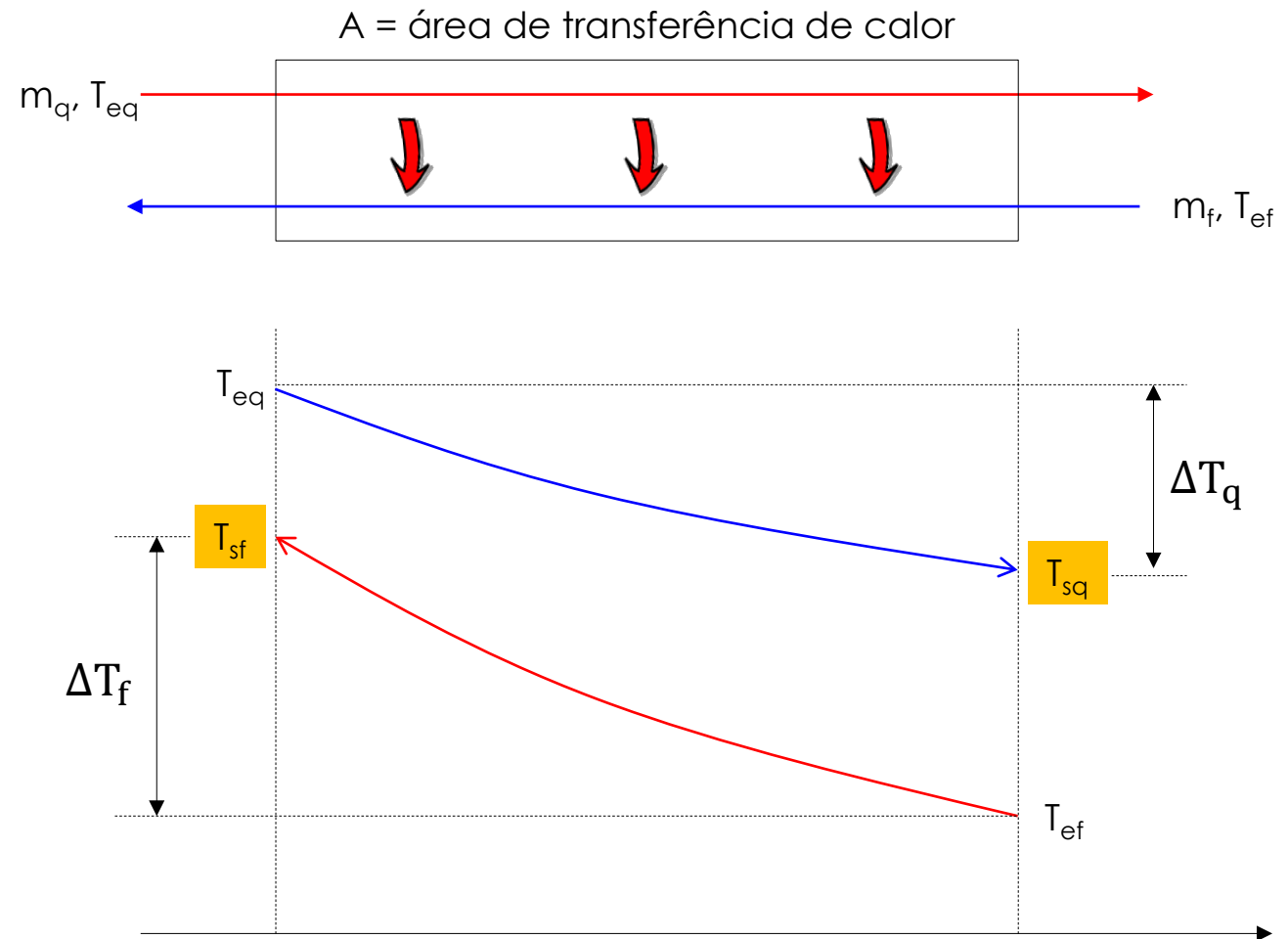
Por que a  $\Delta T_{\text{In}}$  não tende a zero quando  $UA \rightarrow \infty$  ?

$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$



$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

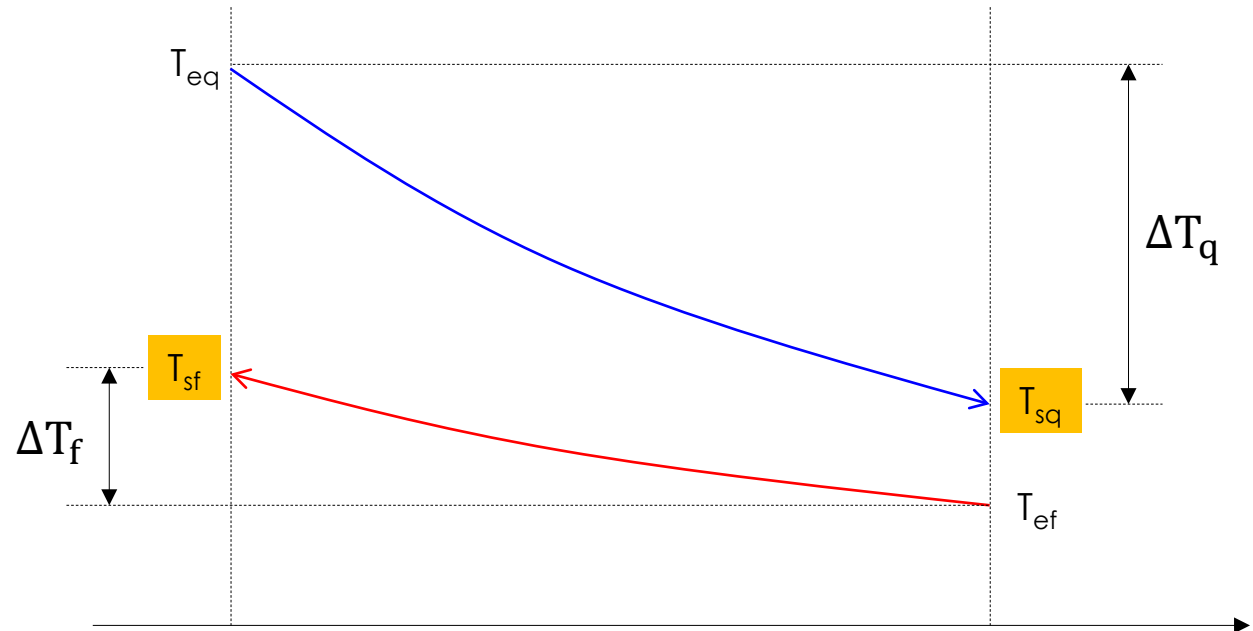
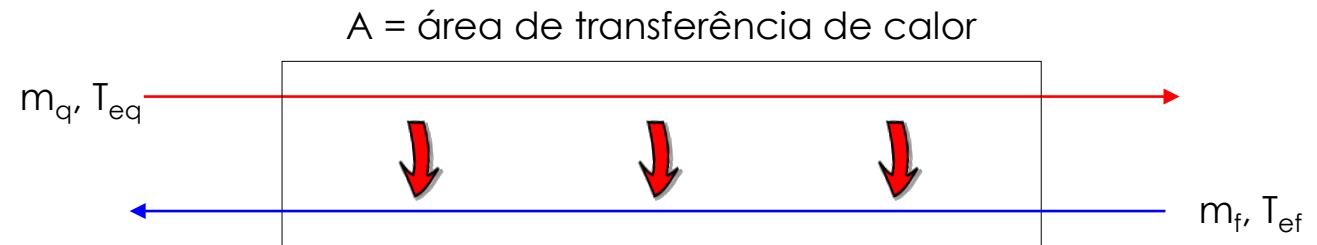
$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$



$$m_q C_{P,q} < m_f C_{P,f} \rightarrow \Delta T_q > \Delta T_f$$





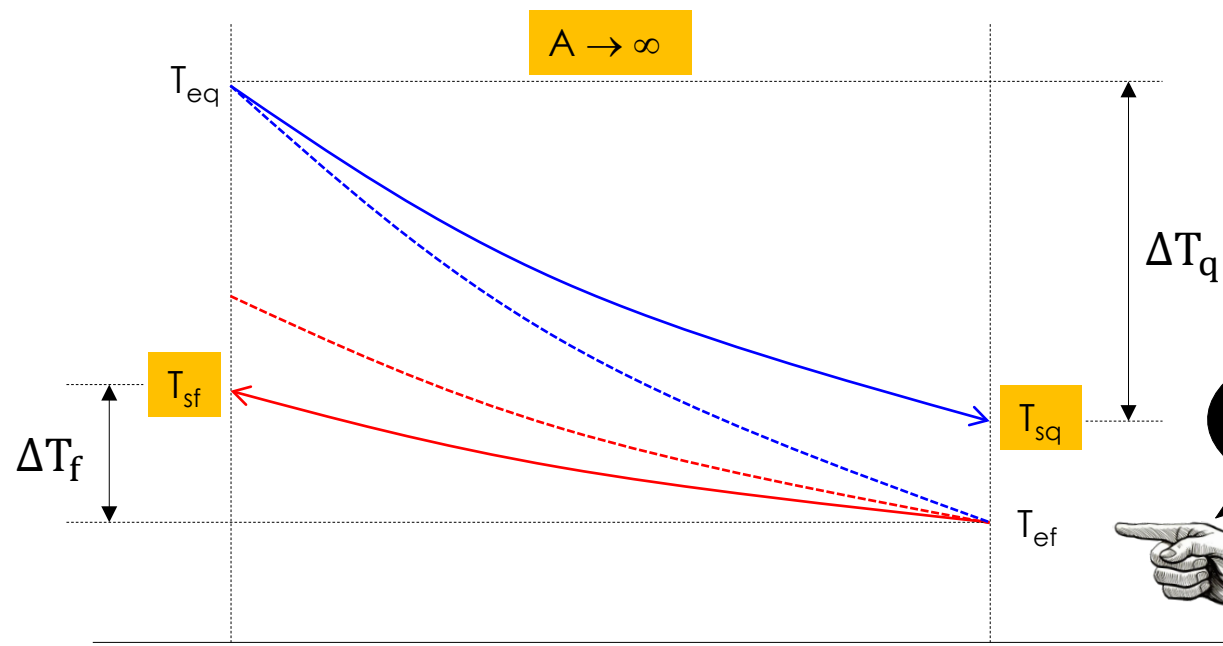
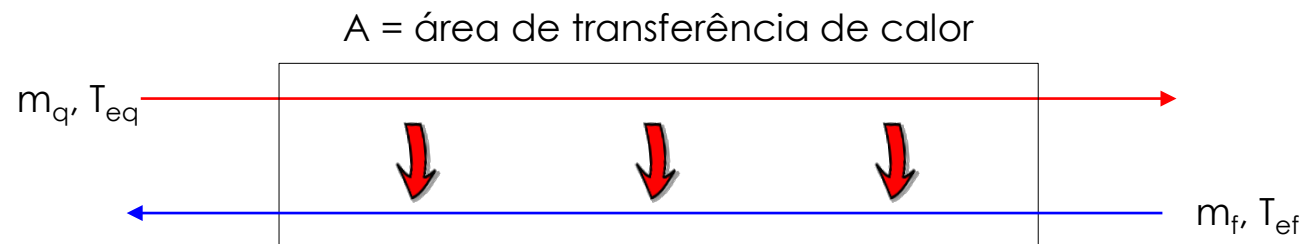
$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$

$$m_q C_{P,q} < m_f C_{P,f} \rightarrow \Delta T_q > \Delta T_f$$



Vc já explicou isso 5 vezes !!!

$$A \rightarrow \infty \Rightarrow T_{sq} \rightarrow T_{ef}$$

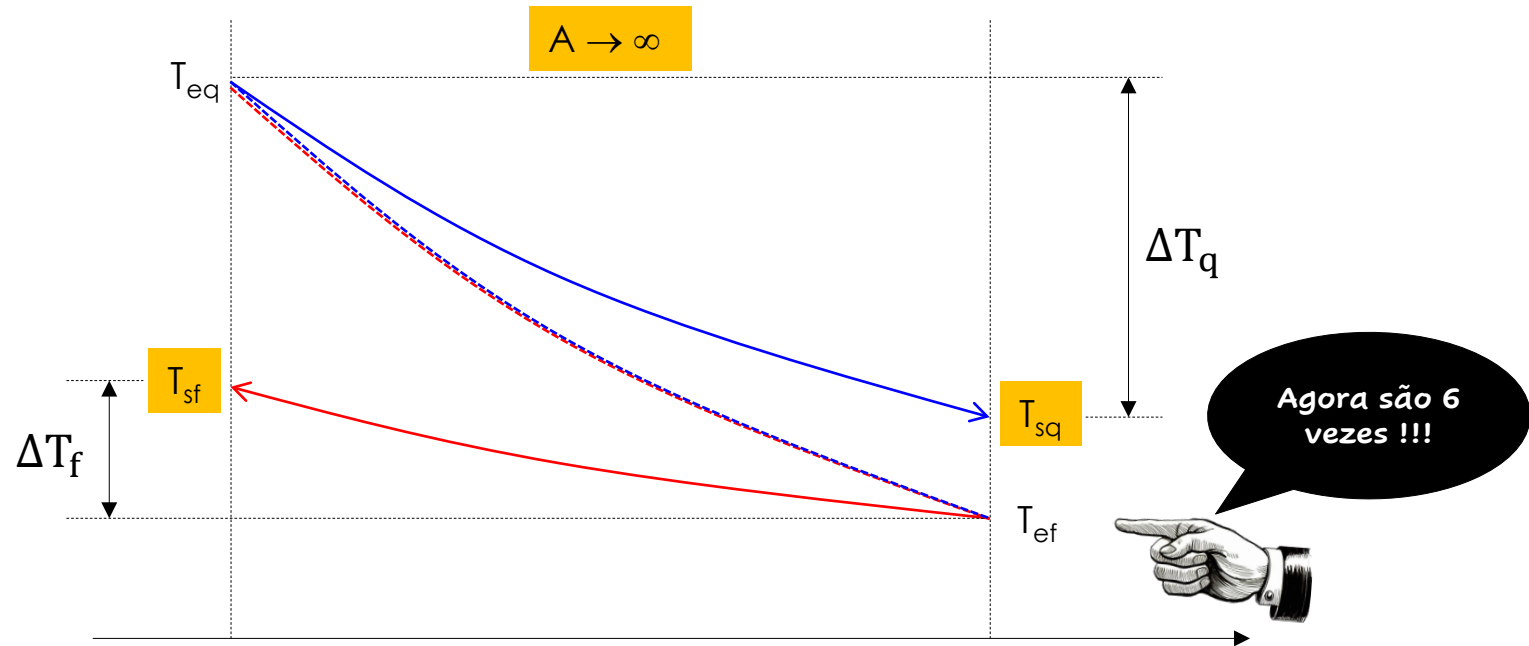
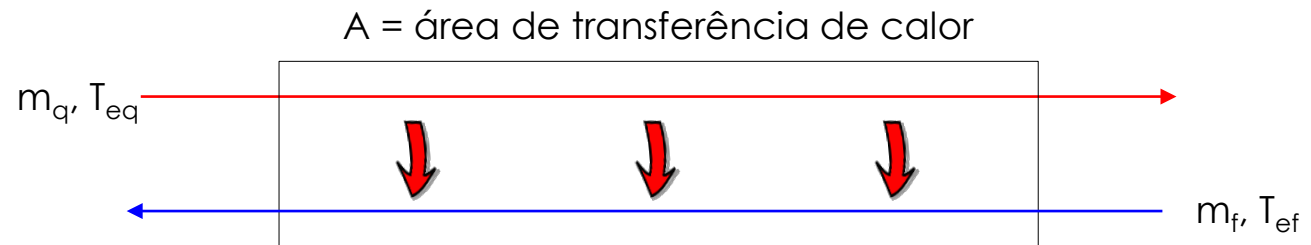
$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$



$$m_q C_{P,q} = m_f C_{P,f} \rightarrow \Delta T_q = \Delta T_f$$

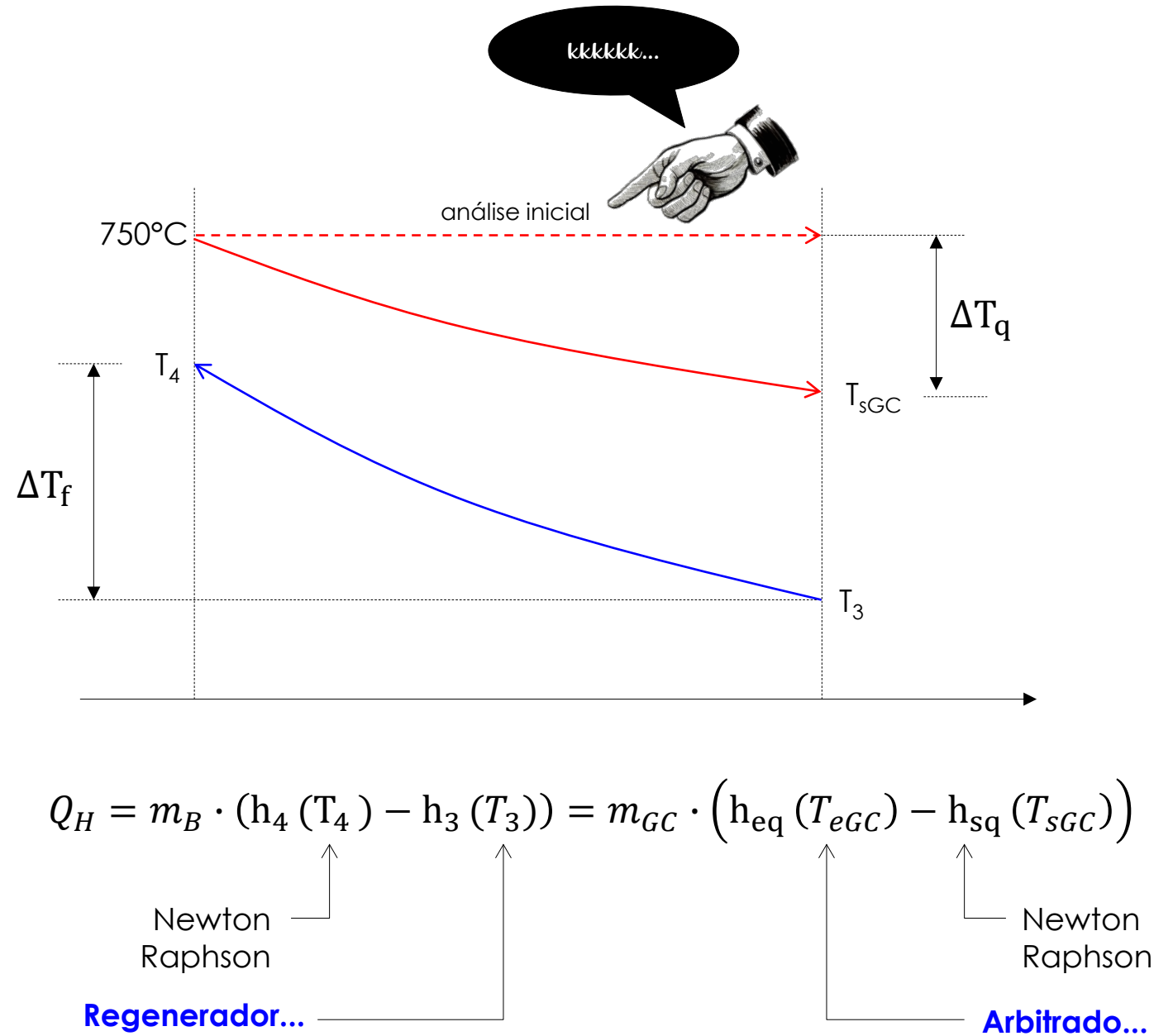
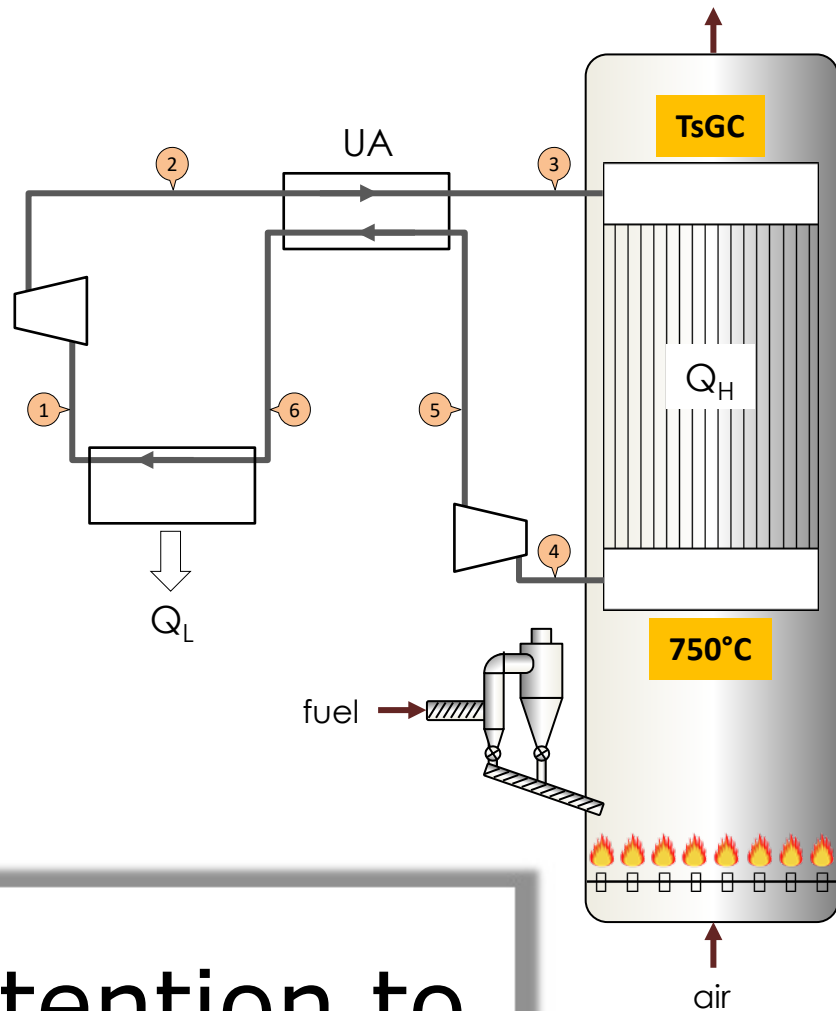


$$A \rightarrow \infty \Rightarrow T_s - T_f \rightarrow 0$$

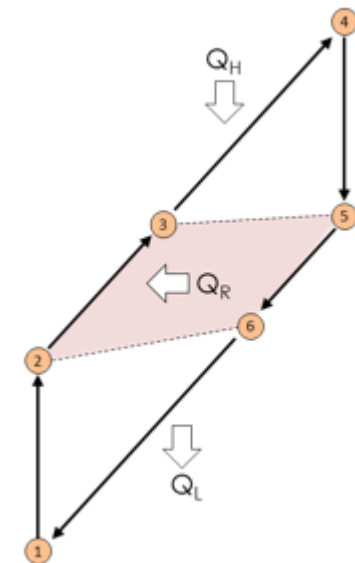
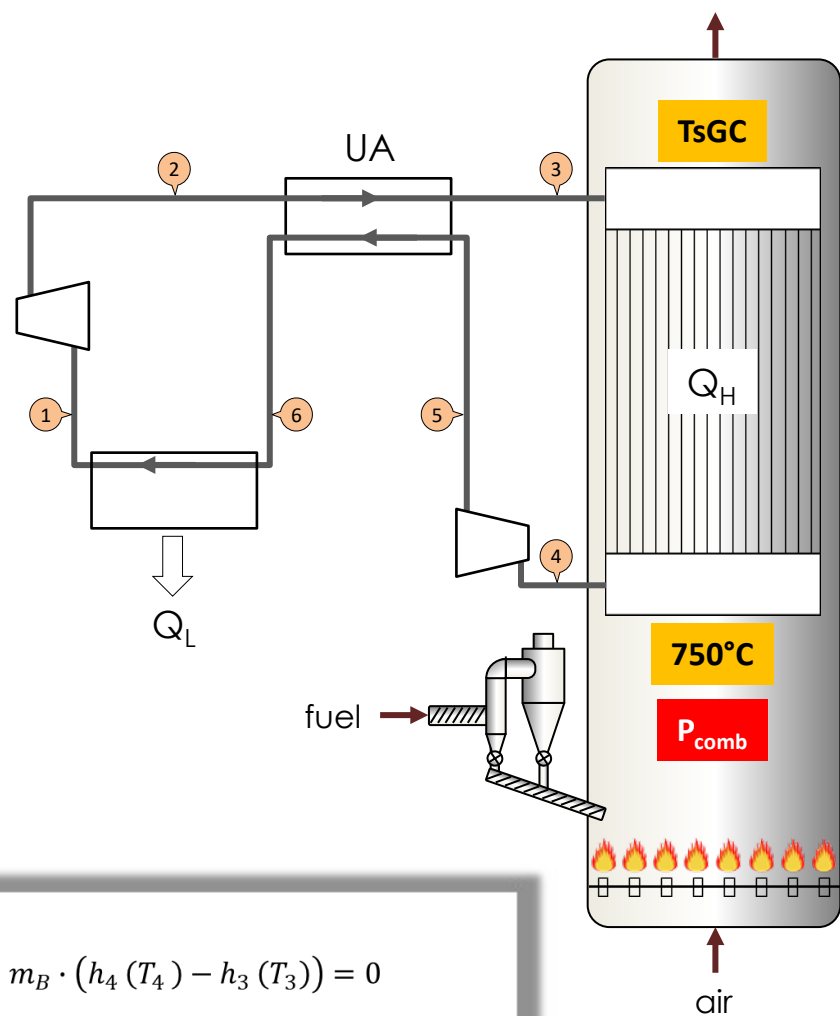
$$A \rightarrow \infty \Rightarrow S_{gen} \rightarrow 0$$

Análise e otimização entrópica da absorção de calor na caldeira ?

# Attention to Filler Words



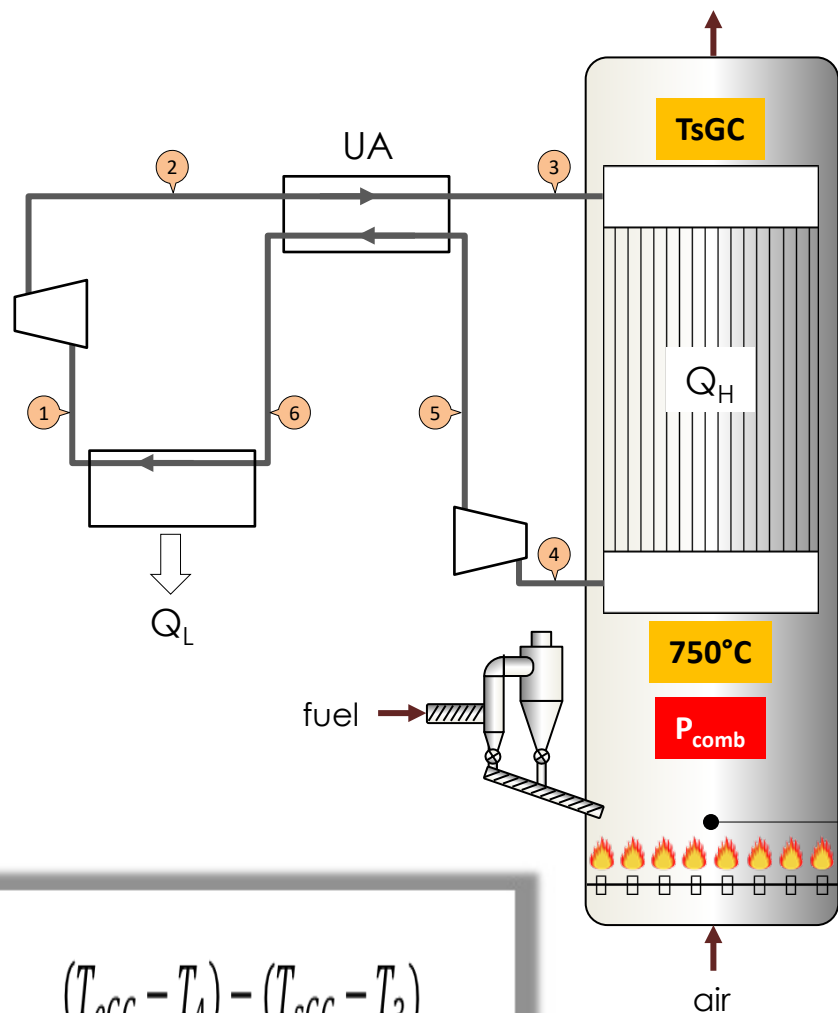




$$f_1 = Q_H - m_B \cdot (h_4(T_4) - h_3(T_3)) = 0$$

$$f_2 = Q_H - m_{GC} \cdot (h_{GC}(T_{eGC}) - h_{GC}(T_{sGC})) = 0$$

$$f_3 = Q_H - UA \frac{(T_{eGC} - T_4) - (T_{sGC} - T_3)}{\ln\left(\frac{T_{eq} - T_4}{T_{sq} - T_3}\right)} = 0$$

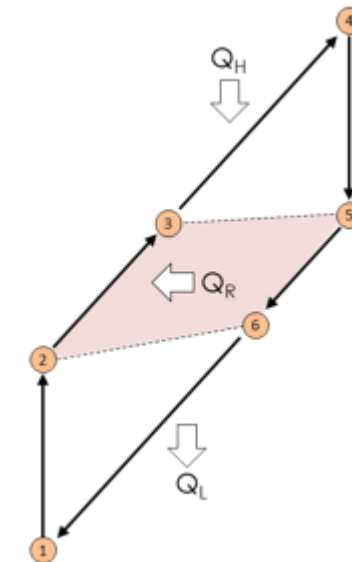


$$f_1 = Q_H - m_B \cdot (h_4(T_4) - h_3(T_3)) = 0$$

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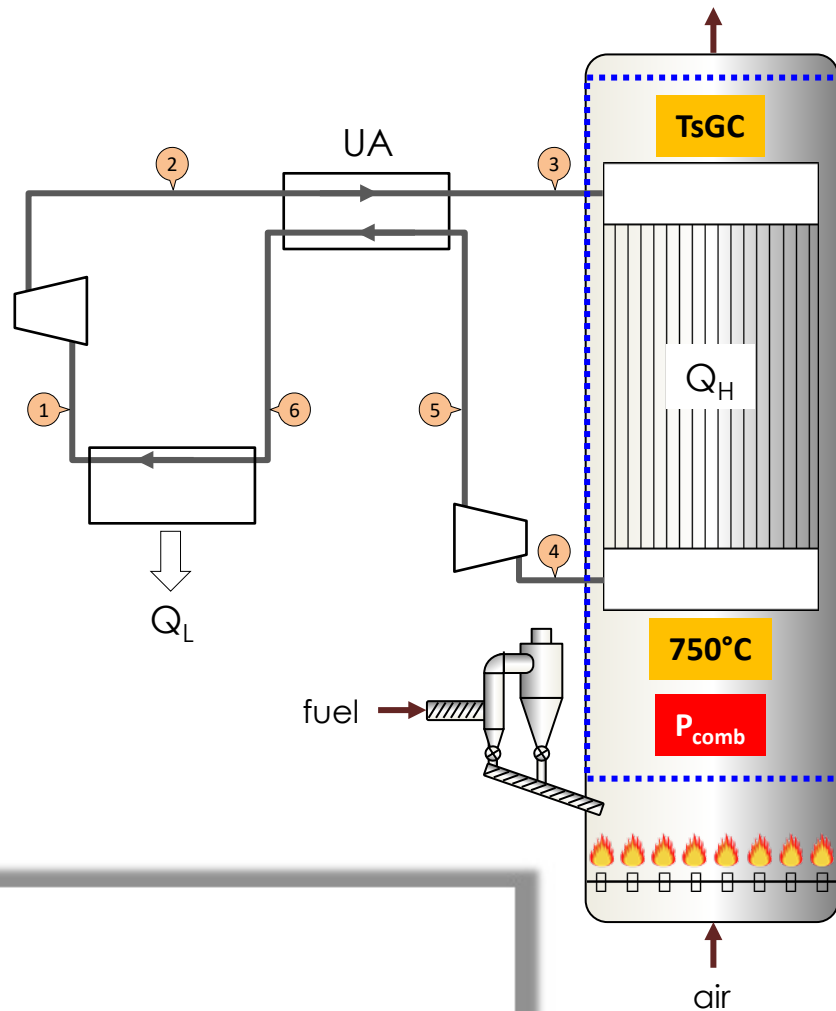
$$f_3 = (T_{eGC} - T_4) - (T_{sGC} - T_3) \cdot \exp\left[\frac{UA}{Q_H}((T_{eGC} - T_4) - (T_{sGC} - T_3))\right] = 0$$



Não adequada p/  
implementação  
numérica

$$f_3 = Q_H - UA \frac{(T_{eGC} - T_4) - (T_{sGC} - T_3)}{\ln\left(\frac{T_{eq} - T_4}{T_{sq} - T_3}\right)} = 0$$

60% CO<sub>2</sub> + 40% H<sub>2</sub>O @ 750°C, P<sub>comb</sub>



## ANÁLISE ENERGÉTICA

$$Q_H = m_B \cdot \overline{C_{P,B}} \cdot (T_4 - T_3) = m_{GC} \cdot \overline{C_{P,GC}} \cdot (T_{eGC} - T_{sGC})$$



$$\frac{m_B \cdot \overline{C_{P,B}}}{m_{GC} \cdot \overline{C_{P,GC}}} = \frac{T_{eGC} - T_{sGC}}{T_4 - T_3}$$

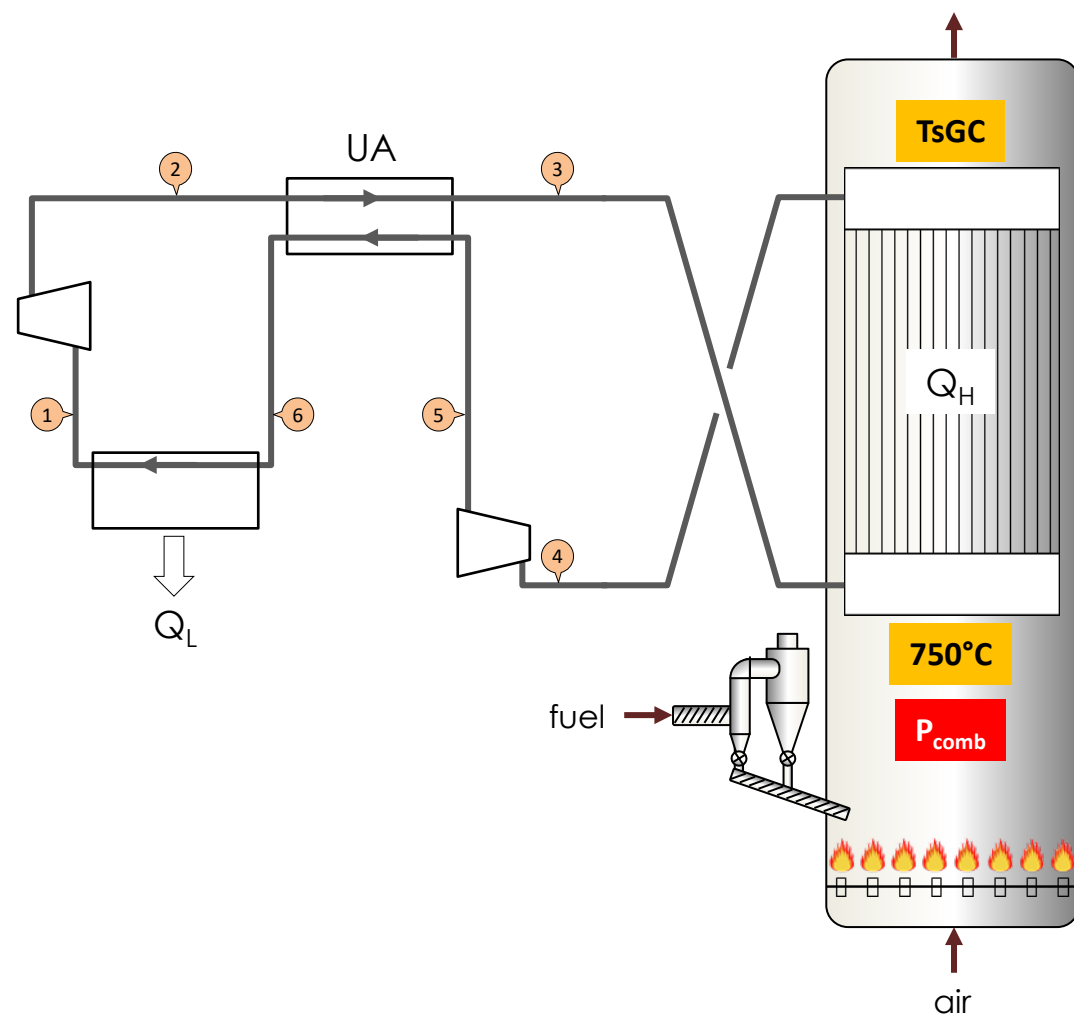
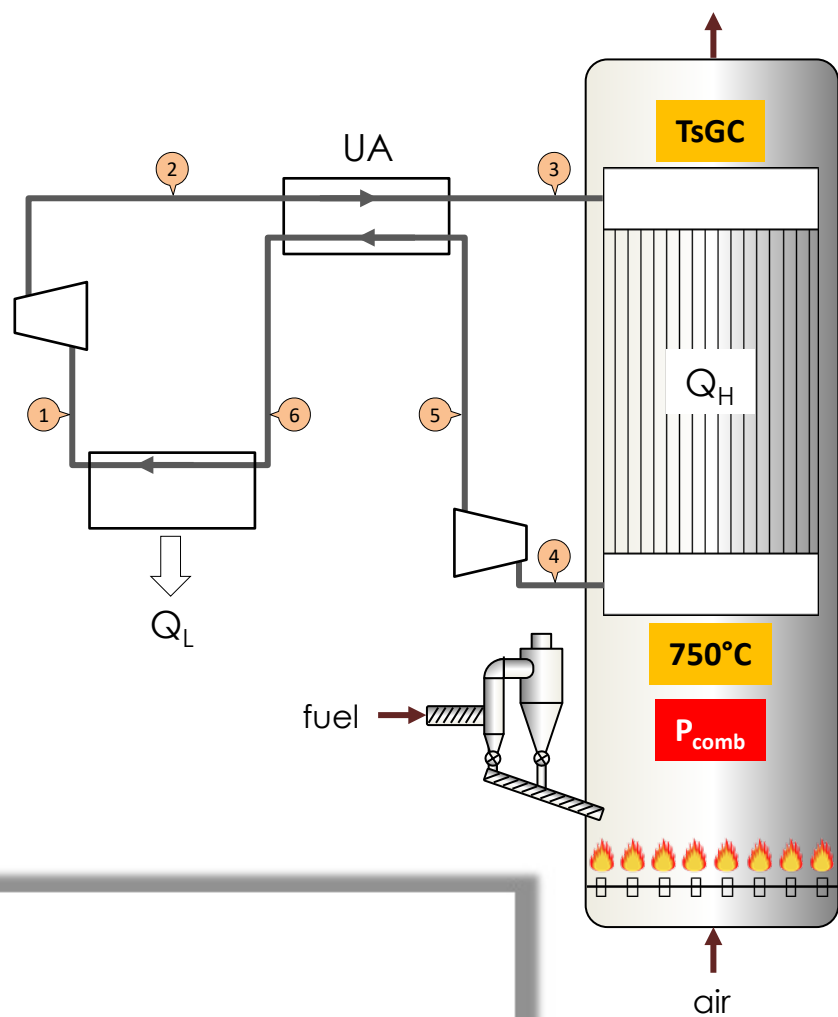
## ANÁLISE ENTRÓPICA

$$\sum \frac{Q_k}{T_k} + \sum m_{i,k} s_{i,k} - \sum m_{o,k} s_{o,k} + S_{gen} = 0$$

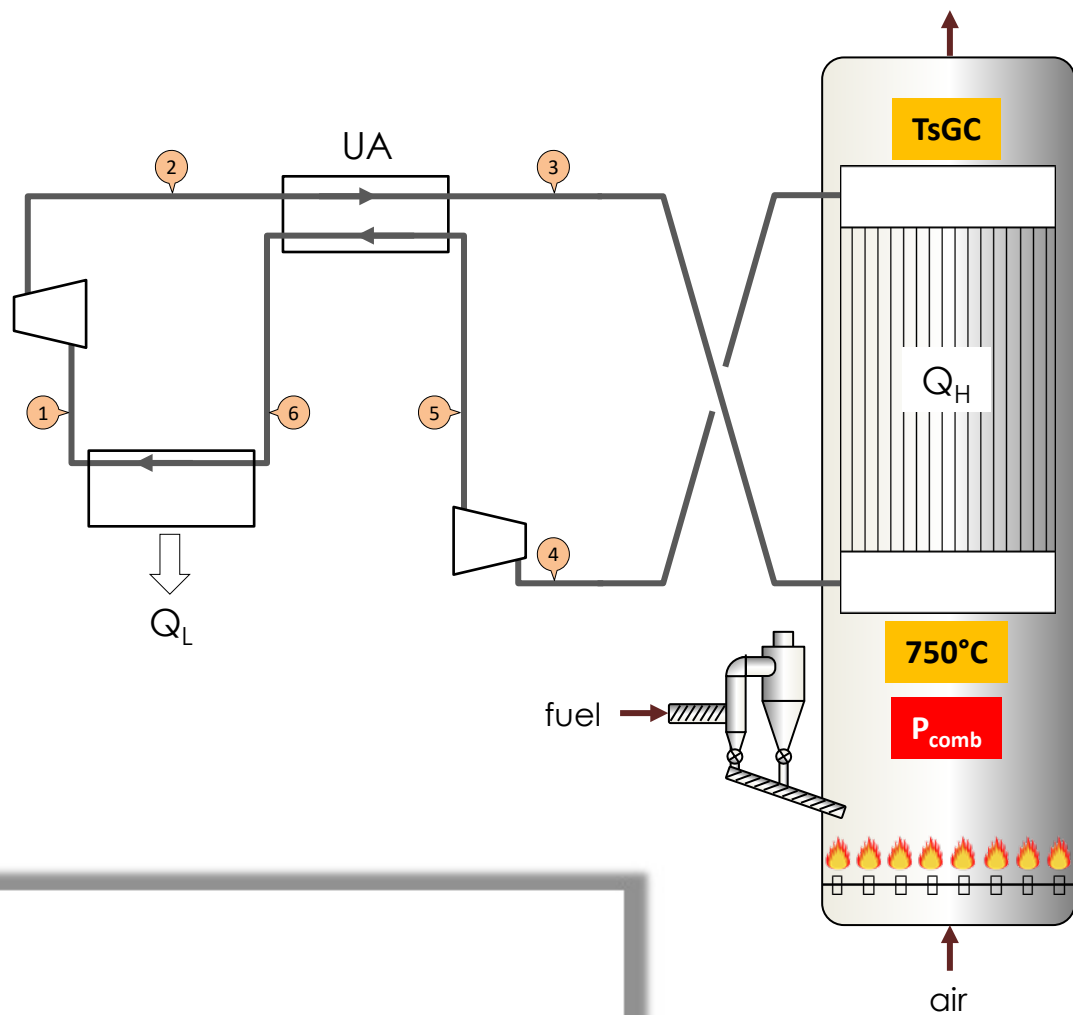
$$S_{gen} = m_B (s_3 - s_4) + m_{GC} (s_{sGC} - s_{eGC})$$

$$\frac{S_{gen}}{m_{GC}} = \frac{m_B}{m_{GC}} (s_3 - s_4) + (s_{sGC} - s_{eGC})$$





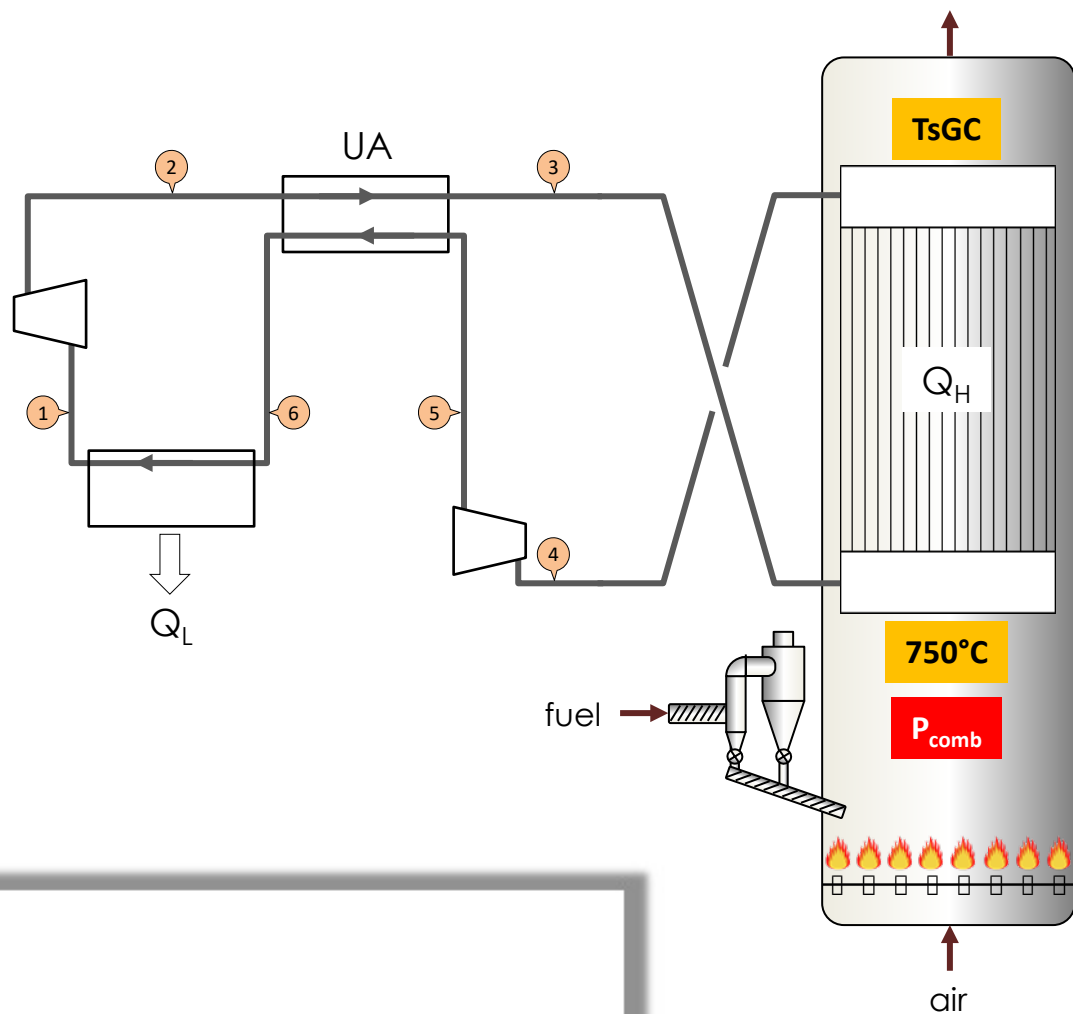




$$f_1 = Q_H - m_B \cdot (h_4(T_4) - h_3(T_3)) = 0$$

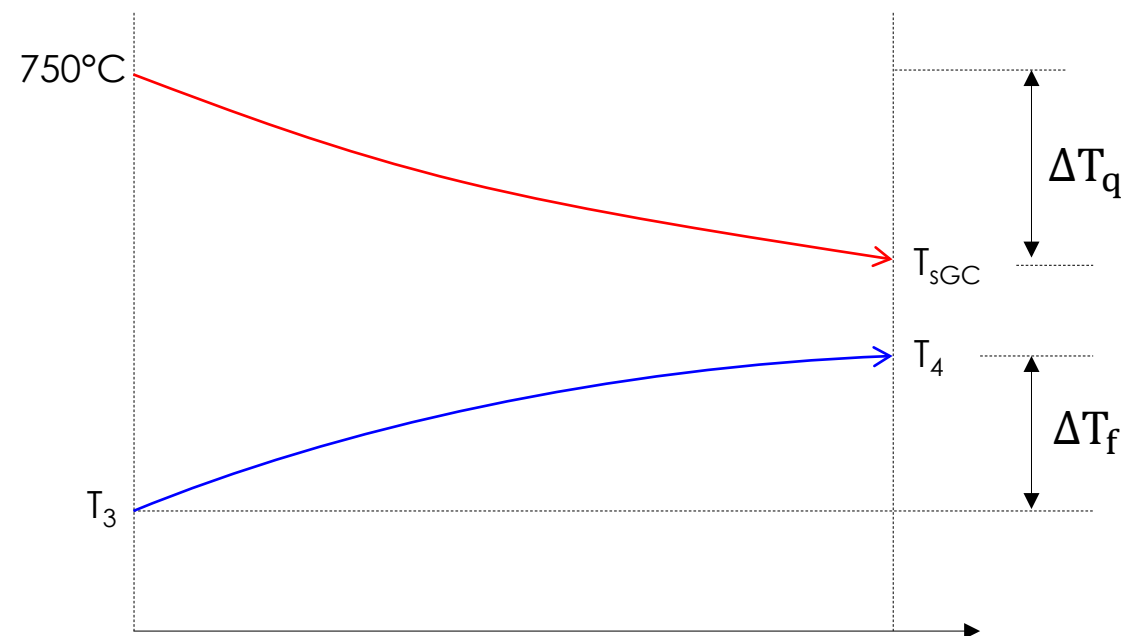
$$f_2 = Q_H - m_{GC} \cdot (h_{GC}(T_{eGC}) - h_{GC}(T_{sGC})) = 0$$

$$f_3 = Q_H - UA \frac{(T_{eGC} - T_3) - (T_{sGC} - T_4)}{\ln\left(\frac{T_{eq} - T_3}{T_{sq} - T_4}\right)} = 0$$



$$f_1 = Q_H - m_B \cdot (h_4(T_4) - h_3(T_3)) = 0$$

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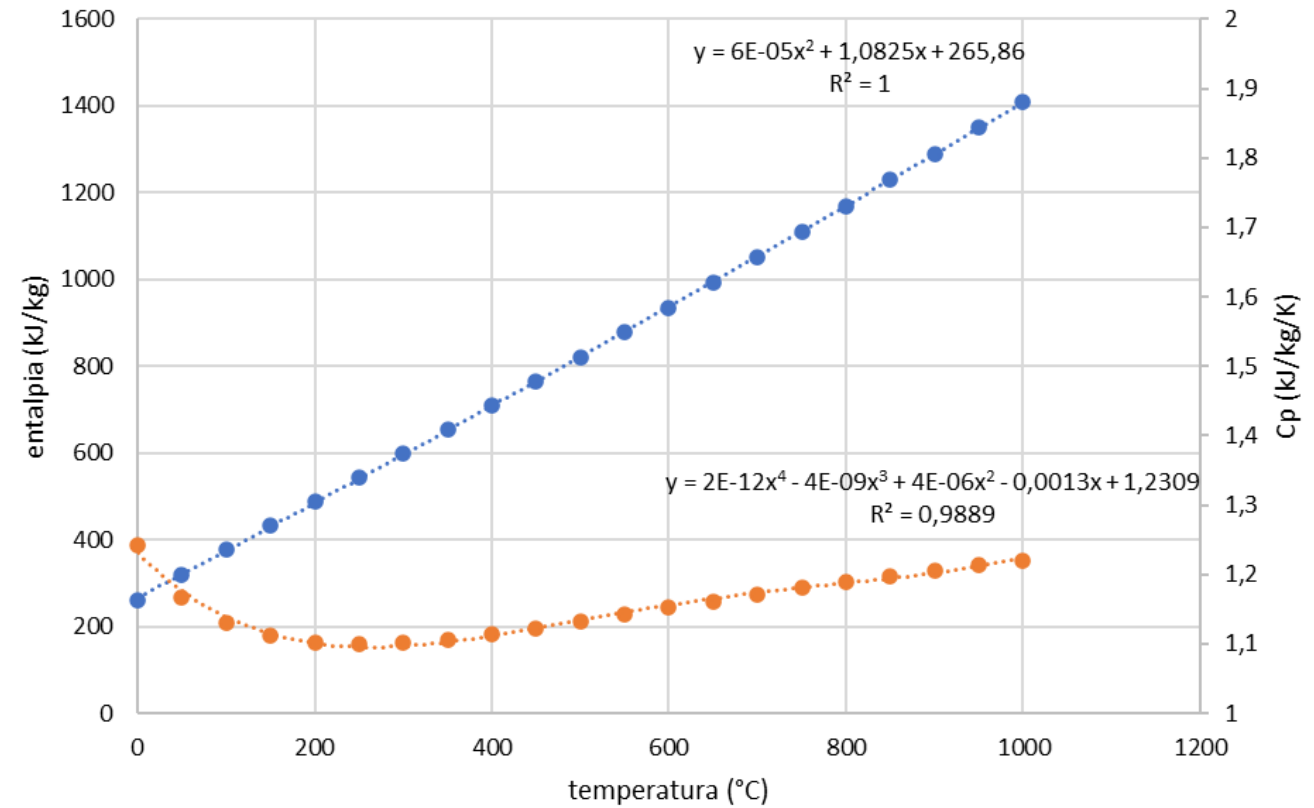


$$f_3 = Q_H - UA \frac{(T_{eGC} - T_3) - (T_{sGC} - T_4)}{\ln \left( \frac{T_{eq} - T_3}{T_{sq} - T_4} \right)} = 0$$

$$f_1 = Q_H - m_B \cdot (h_4(T_4) - h_3(T_3)) = 0$$

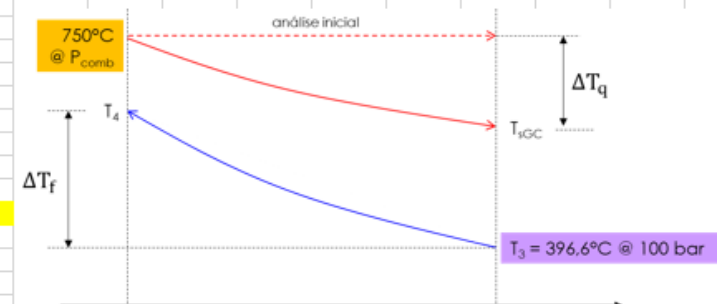
2: nitrogen: p = 100, bar

	Temperature (°C)	Pressure (bar)	Density (kg/m³)	Volume (m³/kg)	Enthalpy (kJ/kg)	Entropy (kJ/kg-K)	Cp (kJ/kg-K)
1	0,00000	100,00	125,25	0,0079842	259,27	5,3024	1,2412
2	50,000	100,00	102,50	0,0097564	319,26	5,5043	1,1676
3	100,00	100,00	87,428	0,011438	376,63	5,6694	1,1309
4	150,00	100,00	76,534	0,013066	432,64	5,8103	1,1116
5	200,00	100,00	68,216	0,014659	487,95	5,9339	1,1023
6	250,00	100,00	61,620	0,016229	542,98	6,0444	1,0997
7	300,00	100,00	56,241	0,017781	597,99	6,1449	1,1016
8	350,00	100,00	51,760	0,019320	653,19	6,2372	1,1067
9	400,00	100,00	47,962	0,020850	708,69	6,3229	1,1139
10	450,00	100,00	44,699	0,022372	764,60	6,4030	1,1225
11	500,00	100,00	41,863	0,023888	820,96	6,4783	1,1320
12	550,00	100,00	39,372	0,025399	877,81	6,5496	1,1419
13	600,00	100,00	37,166	0,026906	935,15	6,6172	1,1518
14	650,00	100,00	35,199	0,028410	992,99	6,6816	1,1617
15	700,00	100,00	33,433	0,029911	1051,3	6,7431	1,1713
16	750,00	100,00	31,837	0,031410	1110,1	6,8021	1,1806
17	800,00	100,00	30,389	0,032907	1169,4	6,8586	1,1894
18	850,00	100,00	29,068	0,034402	1229,0	6,9130	1,1978
19	900,00	100,00	27,859	0,035896	1289,1	6,9653	1,2058
20	950,00	100,00	26,746	0,037388	1349,6	7,0158	1,2132
21	1000,0	100,00	25,720	0,038880	1410,5	7,0645	1,2203



$$h_{@100bar}(T) = C_{P@100bar}(T) \cdot (T - T_{ref})$$

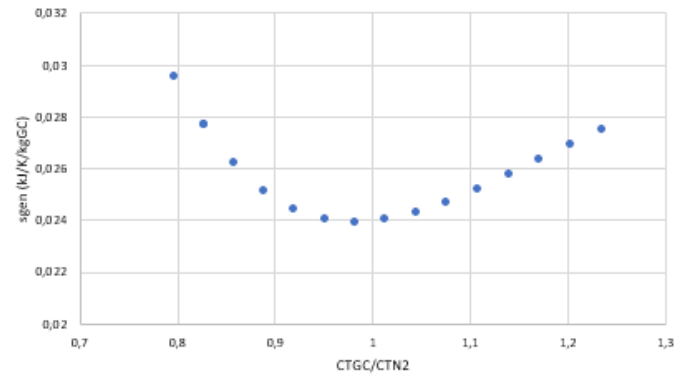
	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	AA
1	compo 1	carbon dioxide	0,6									QH	T4	TsGC													
2	compo 2	water	0,4			QH	3232,2	kW	f1	0	f1	1	-11,68	0													
3	Gcomb	carbon dioxide;0,6;water;0,4			T4	680,17	°C		f2	0	f2	1	0	8,9279													
4	mGC	6,75	kg/s		TsGC	408,08	°C		f3	0	f3	0,039	1,1604	-3,921													
5	TeGC	750	°C									QH	T4	TsGC													
6	PeGC	1	bar					1																			
7	heGC	1883,899901	kJ/kg		QH	3232,2	kW	dQH	0	f1	0,1721	0,7604	1,7315														
8	seGC	5,360979751	kJ/kg/K		T4	680,17	°C	dT3	0	f2	-0,071	0,0651	0,1483														
9					TsGC	408,08	°C	dTsGC	0	f3	-0,019	0,0268	-0,194														
10	Brayton	nitrogen																									
11	mB	10	kg/s																								
12	T3	396,6	°C																								
13	P3	100	bar																								
14	h3	704,9068077	kJ/kg			h3	704,91	kJ/kg	heGC	1883,9	kJ/kg																
15	s3	6,317224274	kJ/kg/K			s3	6,3172	kJ/kg/K	seGC	5,36098	kJ/kg/K																
16						h4	1028,1	kJ/kg	hsGC	1405,06	kJ/kg																
17	m	1	kg/s			s4	6,7191	kJ/kg/K	ssGC	4,79338	kJ/kg/K																
18	UA	100	kW/k																								
19	eps	0,001	-																								
20																											
21	solve	macro = ctr + j				TeGC =	750,00																				
22	gendata	macro = ctr + k																									
23																											
24						dt =	69,83																				
25						T4 =	680,17																				
26																											
27						CTGC/CTN2																					
28							0,8263																				
29							0,8263																				
30							0,8876																				
31							0,9435																				
32							1,0119																				
33							1,0748																				
34							1,138																				
35							1,2015																				
36							0,7958																				
37							0,8569																				
38							0,9185																				
39							0,9806																				
40							1,0433																				
41							1,1063																				
42							1,1697																				
43							1,2333																				
44																											



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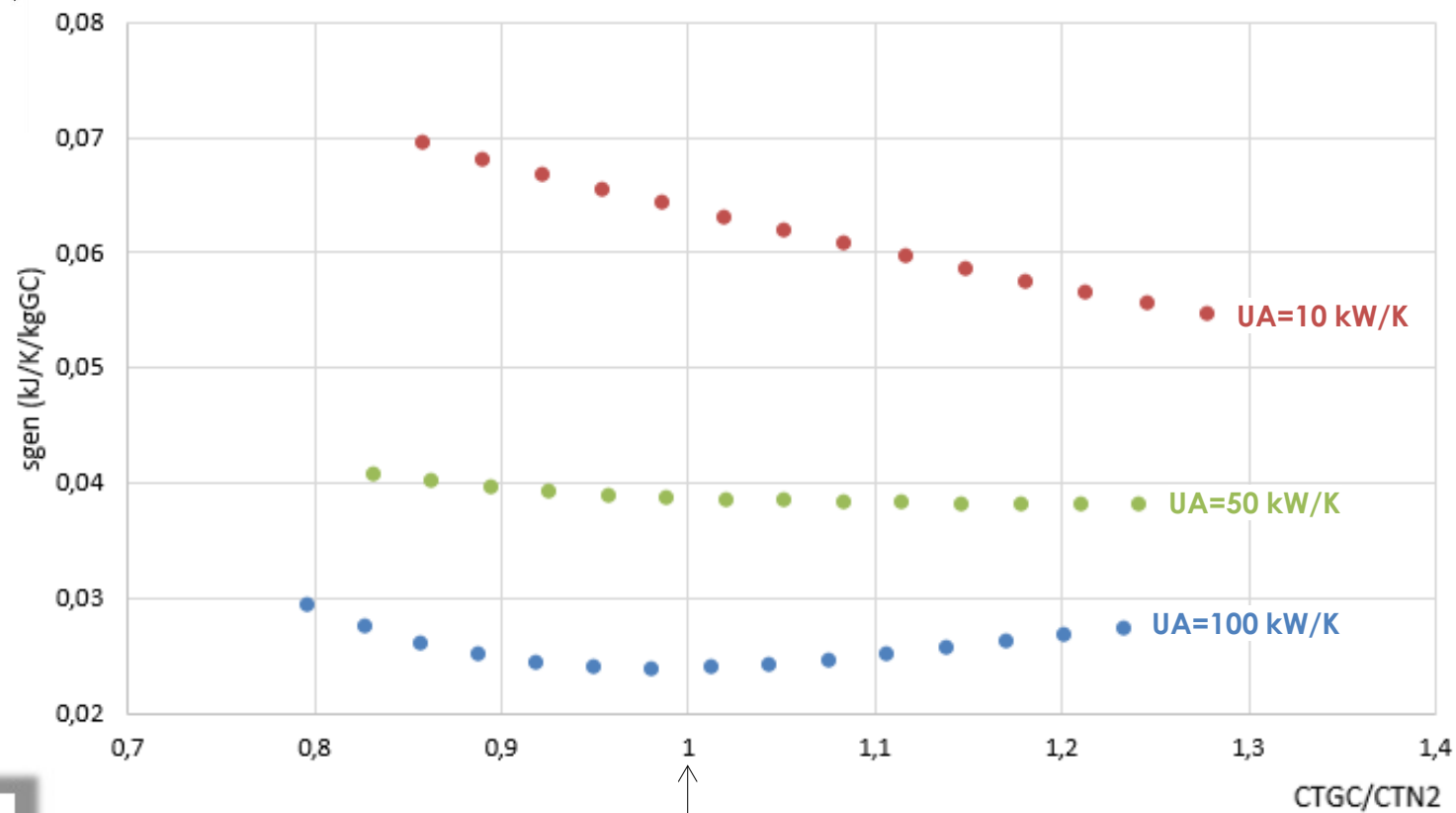
$$f_3 = (T_{eGC} - T_4) - (T_{sGC} - T_3) \exp \left[ \frac{UA}{Q_H} ((T_{eGC} - T_4) - (T_{sGC} - T_3)) \right] = 0$$







$$\frac{S_{gen}}{m_{GC}} = \frac{m_B}{m_{GC}} (s_3 - s_4) + (s_{sGC} - s_{eGC})$$



$$\bar{C}_P \cong \frac{C_{P@Tx} + C_{P@Ty}}{2}$$

$$\frac{m_B \cdot \bar{C}_{P,B}}{m_{GC} \cdot \bar{C}_{P,GC}} = \frac{T_{eGC} - T_{sGC}}{T_4 - T_3}$$

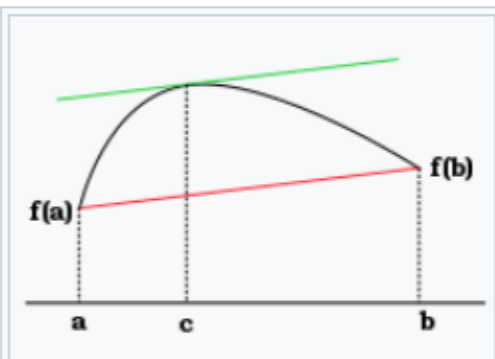
Projeto "sintonizado"

# Teorema do valor médio

🌐 52 línguas ▾

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O teorema do valor médio<sup>[1]</sup>

Em [matemática](#), o **teorema do valor médio** (também conhecido como **Teorema de Lagrange**) afirma que, dada uma [função contínua](#)  $f$  definida num intervalo fechado  $[a, b]$  e [diferenciável](#) em  $(a, b)$ , existe algum ponto  $c$  em  $(a, b)$  tal que

$$f'(c) = \frac{f(b) - f(a)}{b - a}. \quad \int_a^b f(x) dx = f(c)(b - a).$$

Geometricamente, isto significa que a [tangente](#) ao gráfico de  $f$  no ponto de [abscissa](#)  $c$  é [paralela](#) à [secante](#) que passa pelos pontos de abscissas  $a$  e  $b$ .

O teorema do valor médio também tem uma interpretação em termos físicos: se um objeto está em movimento e se a sua velocidade média é  $v$ , então, durante esse percurso (intervalo  $[a, b]$ ), há um instante (ponto  $c$ ) em que a velocidade instantânea também é  $v$ .

## Cálculo

[Teorema fundamental](#)

[Limite de funções](#)

[Continuidade](#)

[Teorema do valor médio](#)

[Teorema de Rolle](#)

[Cálculo](#)

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[Cálculo integral](#)

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[Cálculo vetorial](#)

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[Cálculo com múltiplas variáveis](#)

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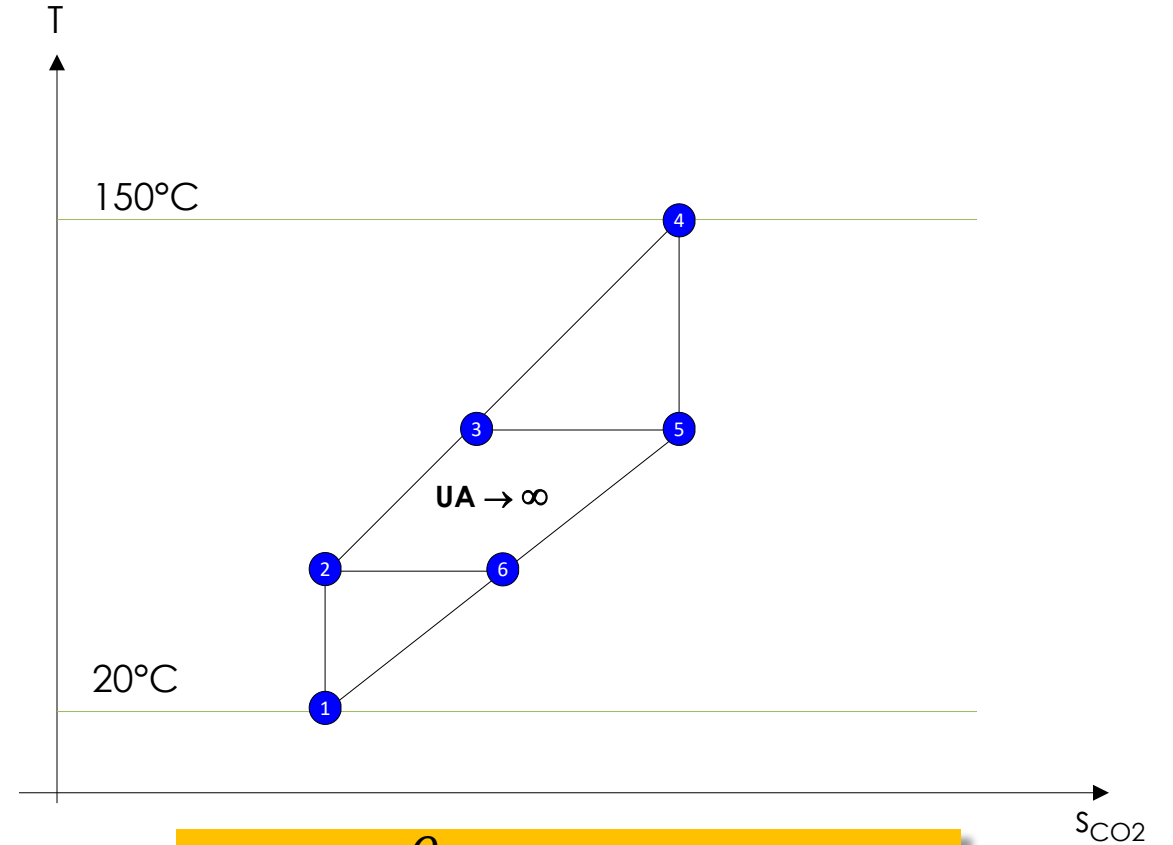
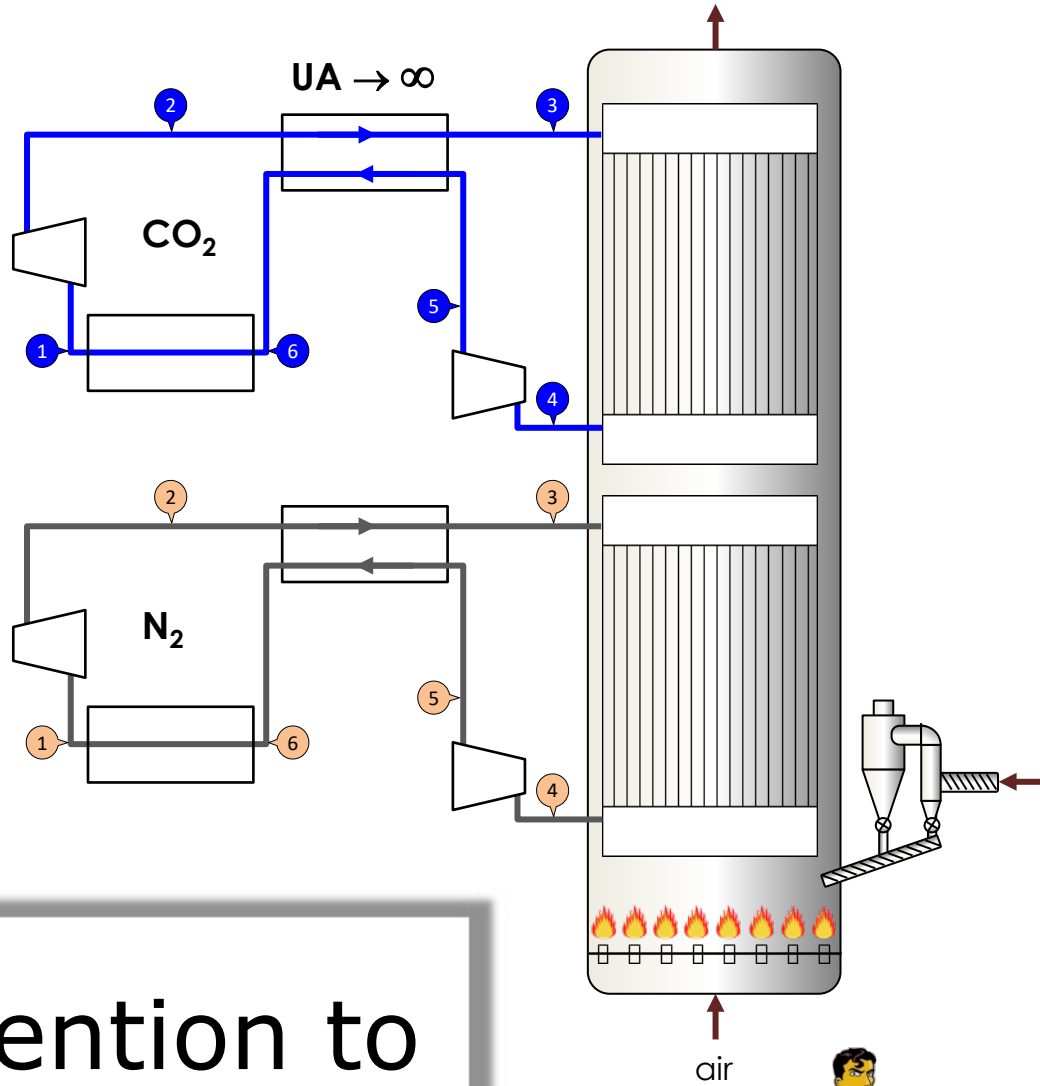
[Cálculo especializado](#)

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V · D · E

$$c \neq \frac{a + b}{2} \rightarrow c \cong \frac{a + b}{2}$$

O comportamento anômalo do CO<sub>2</sub> na região crítica...



$$S_{\text{gen}} = -\sum \frac{Q_k}{T_k} - \sum m_{i,k} s_{i,k} + \sum m_{o,k} s_{o,k}$$

Attention to  
Filler Words



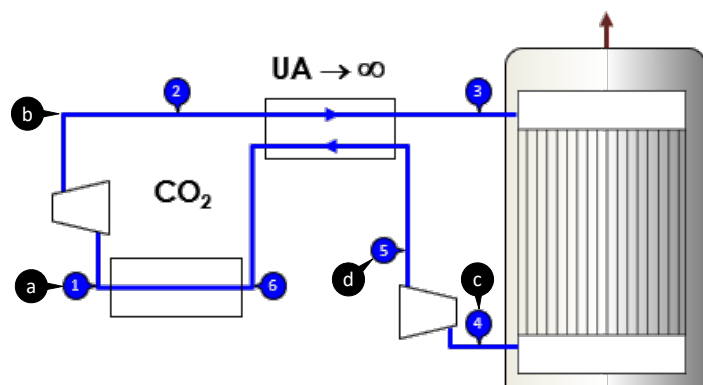
$$\frac{S_{\text{gen,VC}}}{m_B} = -\left(\frac{q_{34}}{T_H} + \frac{q_{61}}{T_L}\right) \quad \frac{S_{\text{gen,regen}}}{m_B} = (s_3 + s_6) - (s_2 + s_5)$$



12: carbon dioxide: Specified state points

	Temperature (°C)	Pressure (bar)	Density (kg/m³)	Enthalpy (kJ/kg)	Entropy (kJ/kg-K)	Quality (kg/kg)
1	20,000	60,000	782,65	254,28	1,1811	Subcooled
2	37,448	200,00	853,18	271,31	1,1811	Undefined
3	150,00	200,00	327,10	523,19	1,8796	Undefined
4	46,086	60,000	140,12	462,28	1,8796	Superheated
5						

$$\eta = \frac{(h_c - h_d) - (h_b - h_a)}{h_c - h_b} = 17.42\%$$

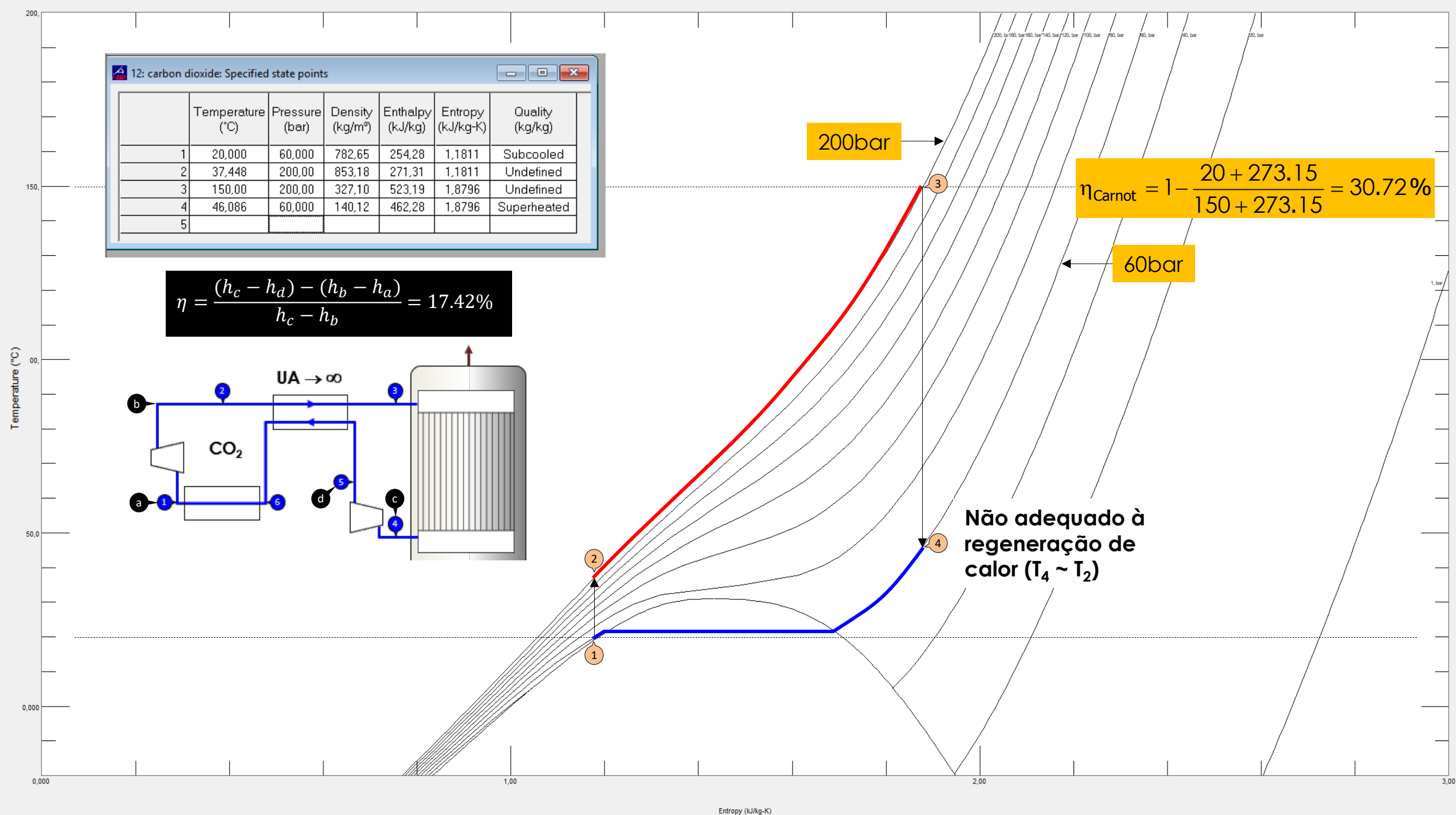


200bar

60bar

$$\eta_{\text{Carnot}} = 1 - \frac{20 + 273.15}{150 + 273.15} = 30.72\%$$

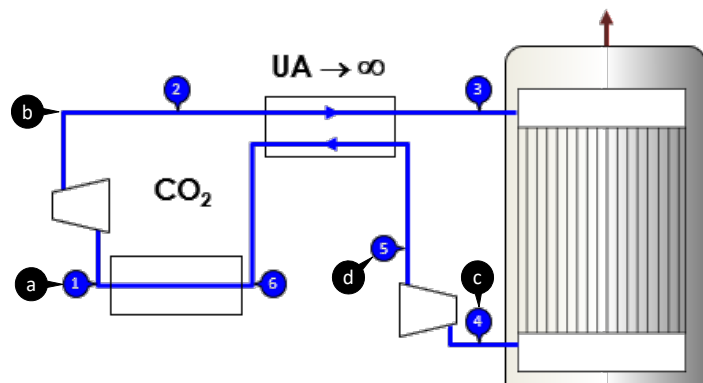
Não adequado à regeneração de calor ( $T_4 \sim T_2$ )



12: carbon dioxide: Specified state points

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5						

$$\eta = \frac{(h_c - h_d) - (h_b - h_a)}{h_c - h_b} = 8,98\%$$

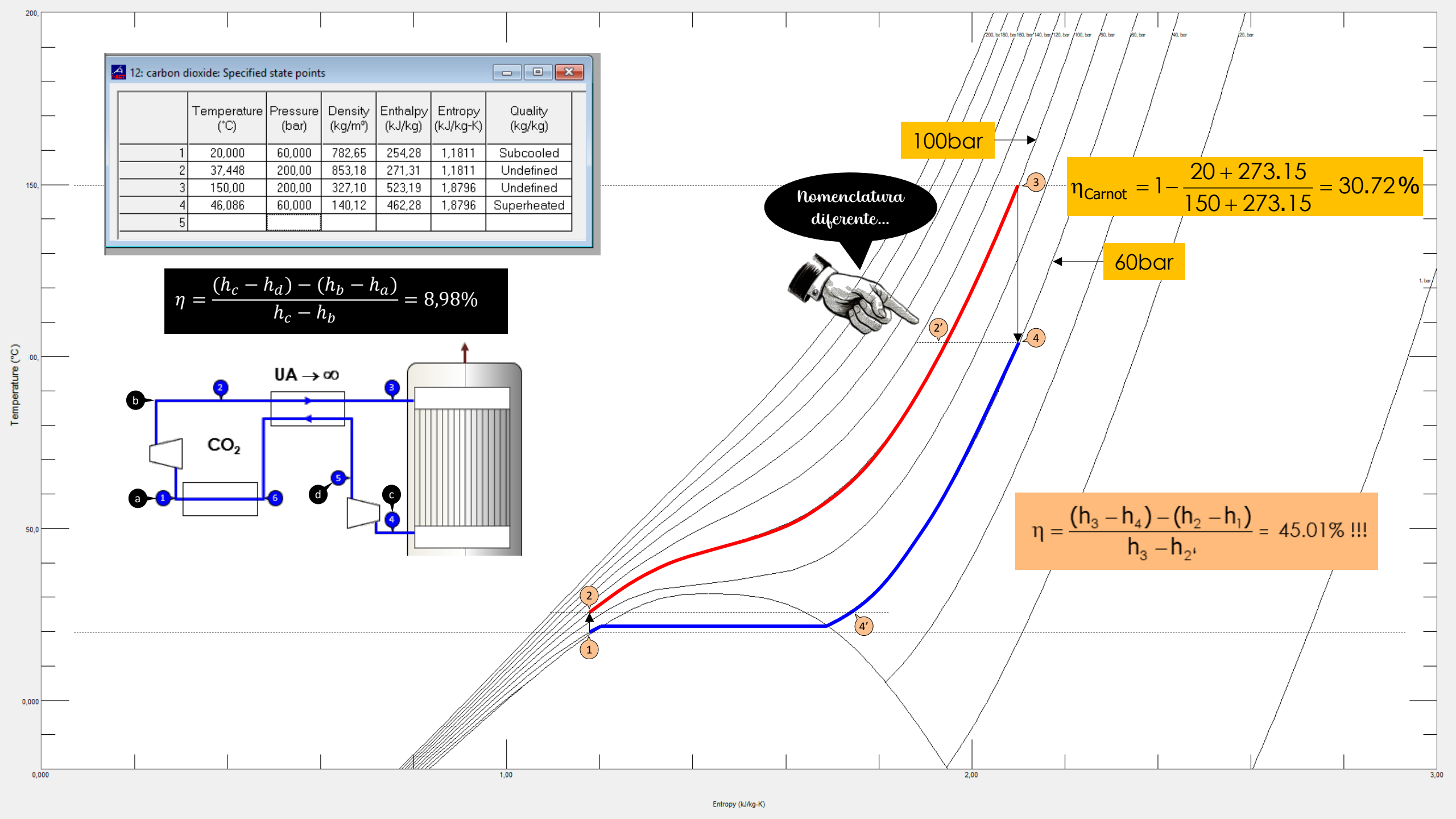


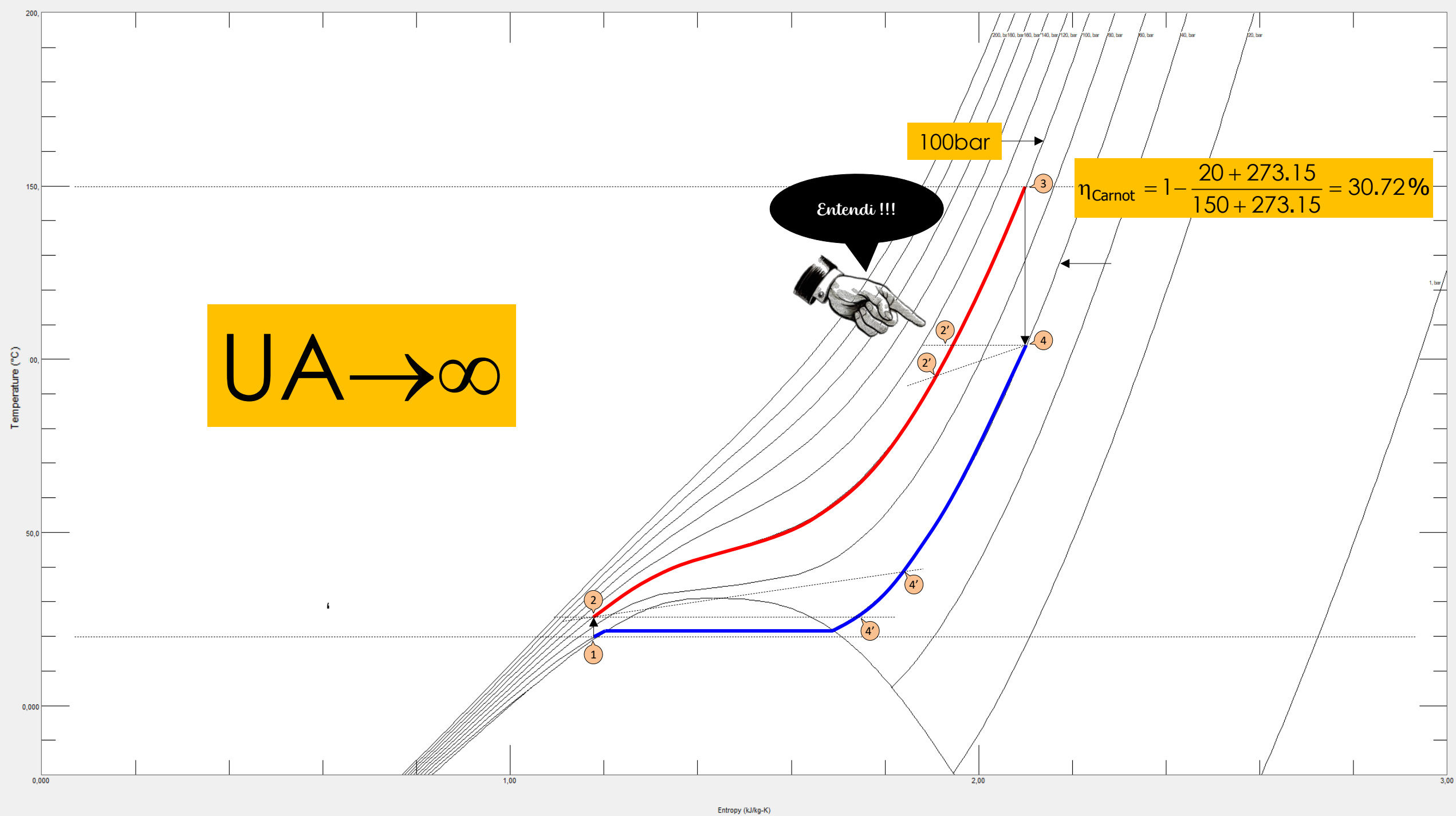
100bar

$$\eta_{\text{Carnot}} = 1 - \frac{20 + 273.15}{150 + 273.15} = 30.72\%$$

60bar

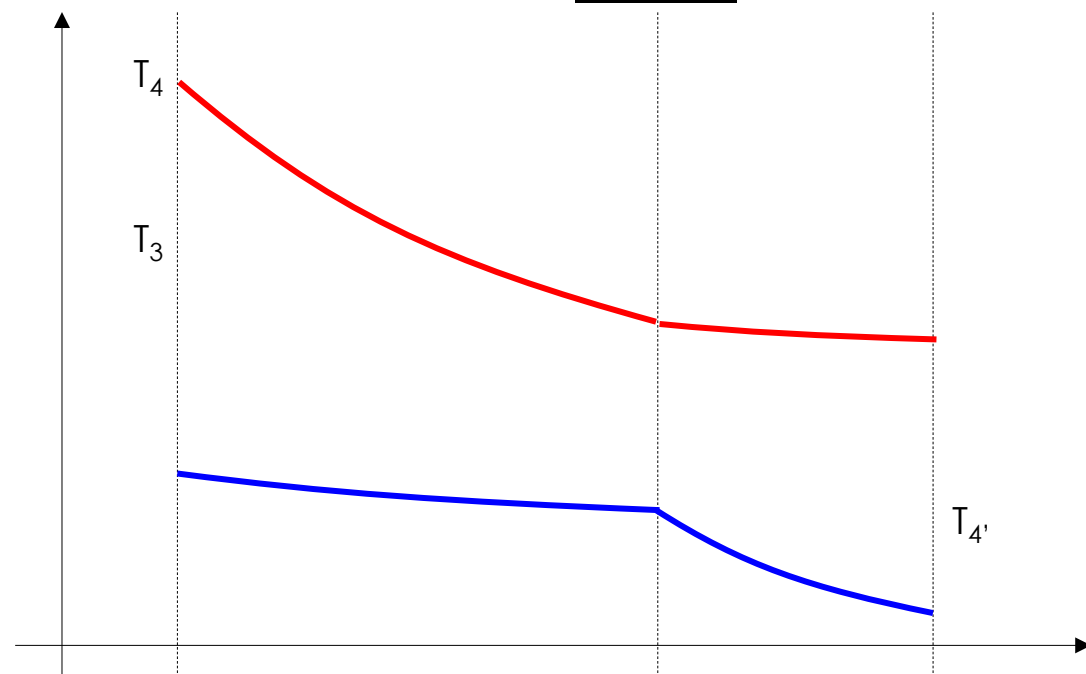
$$\eta = \frac{(h_3 - h_4) - (h_2 - h_1)}{h_3 - h_{2'}} = 45.01\% !!!$$



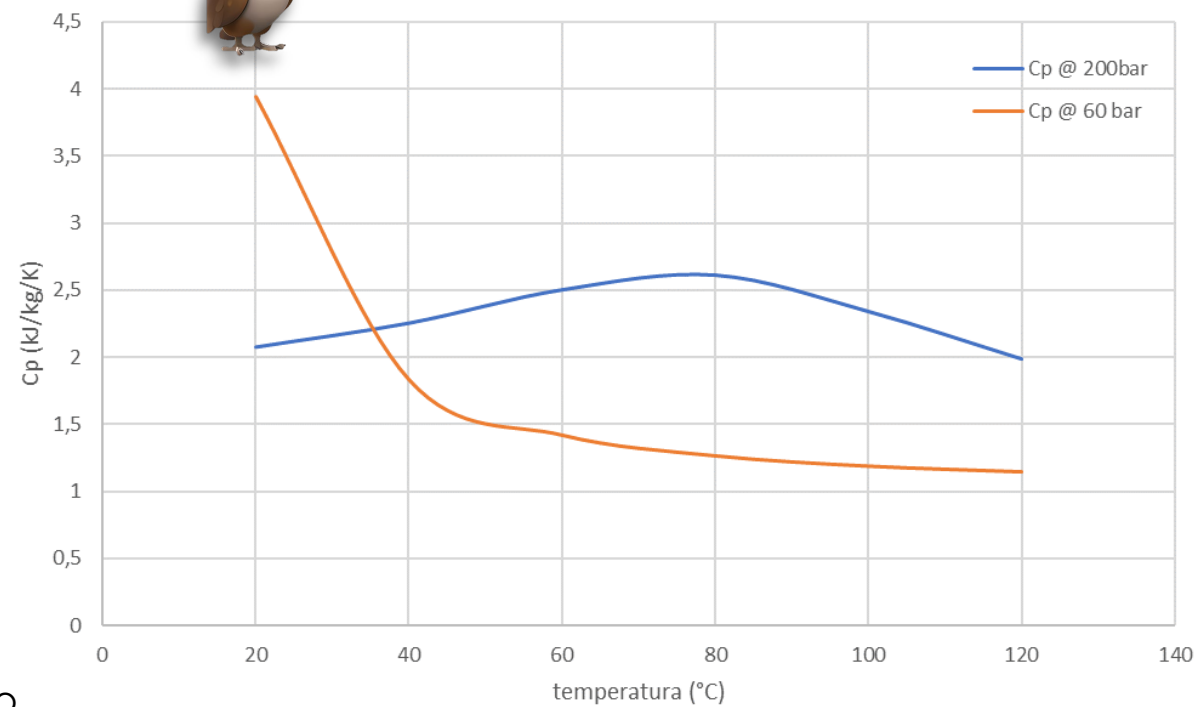


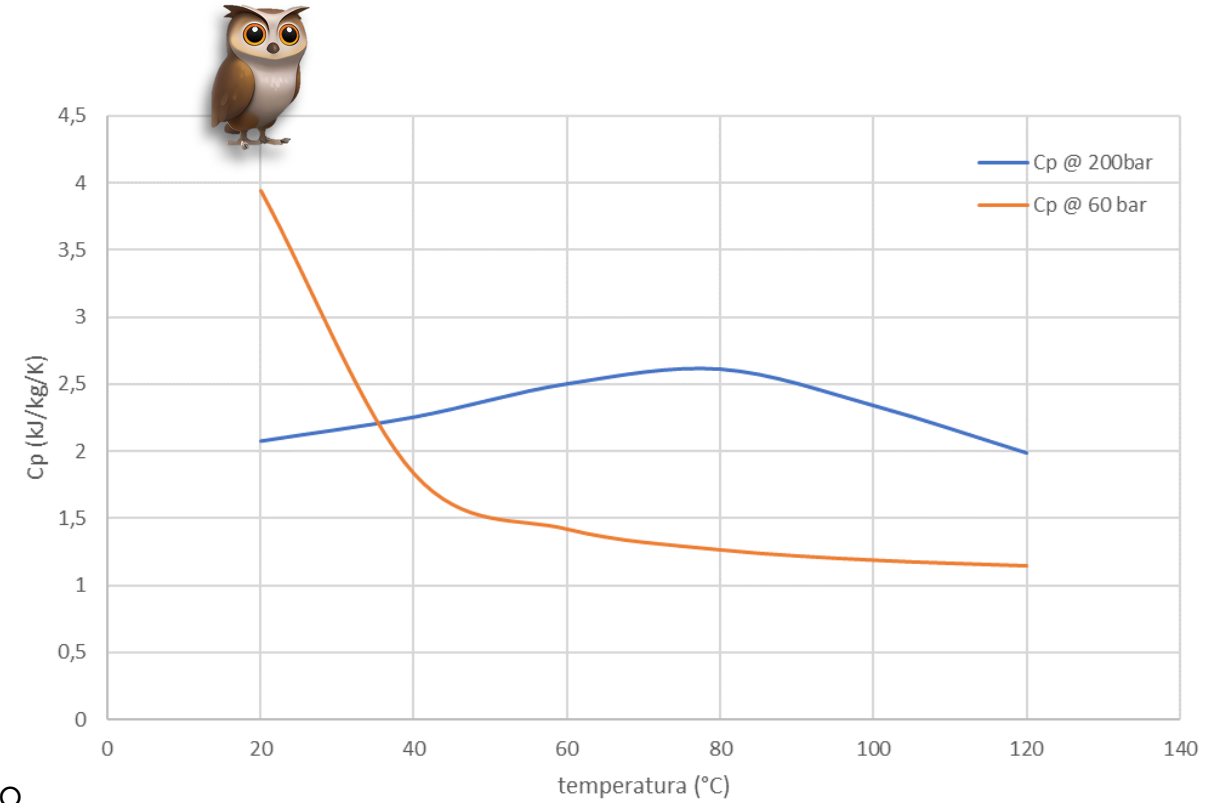
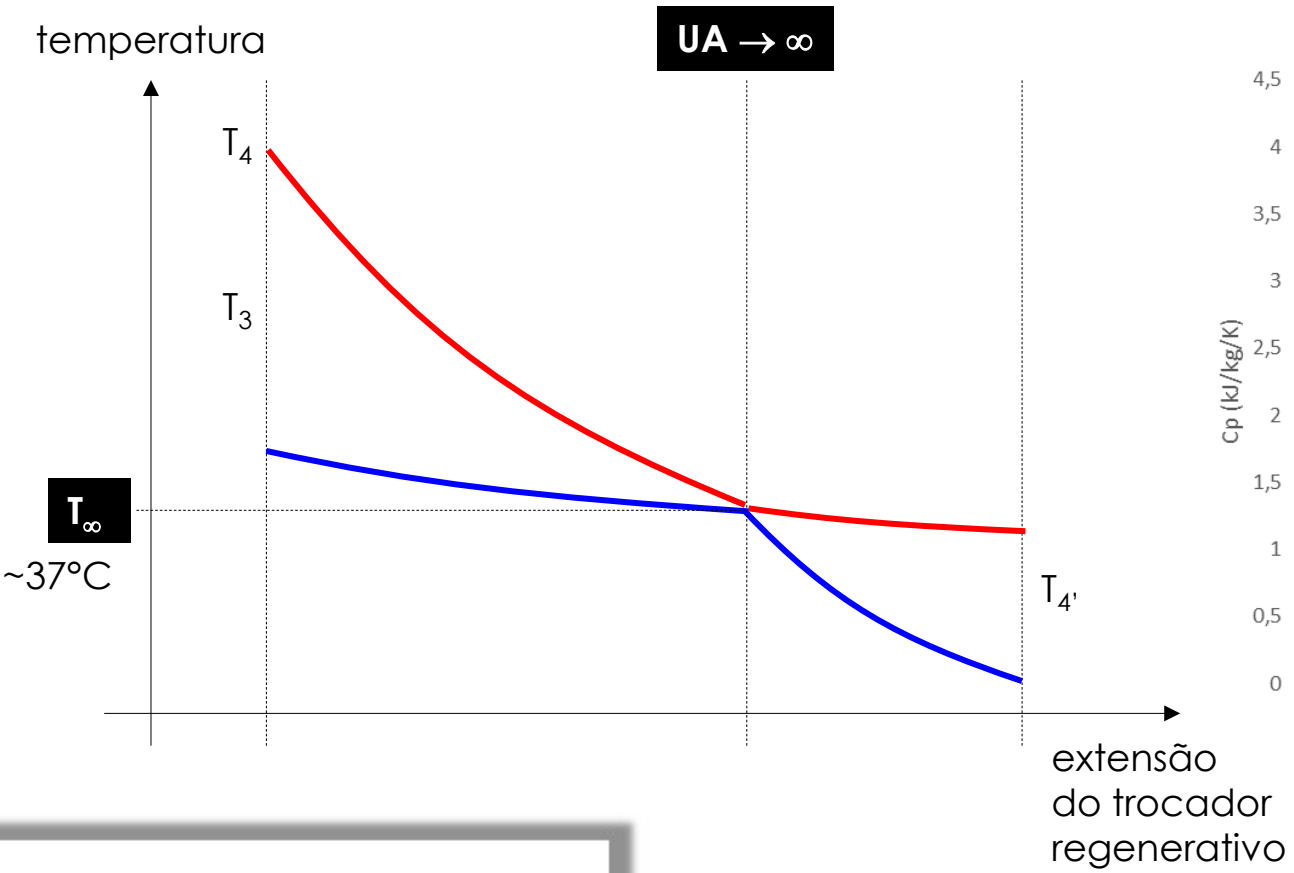
temperatura

$$UA < \infty$$

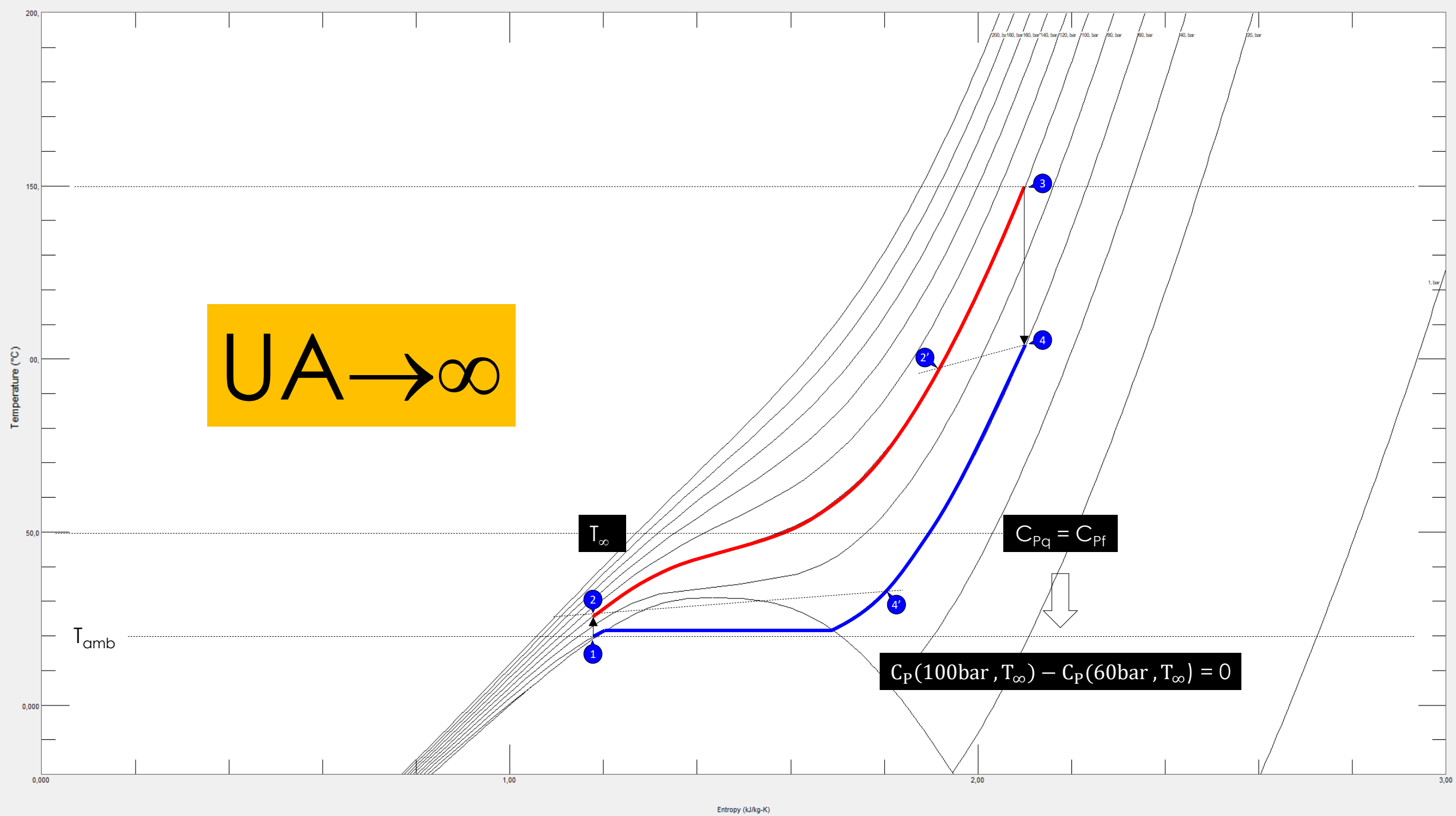


extensão  
do trocador  
regenerativo









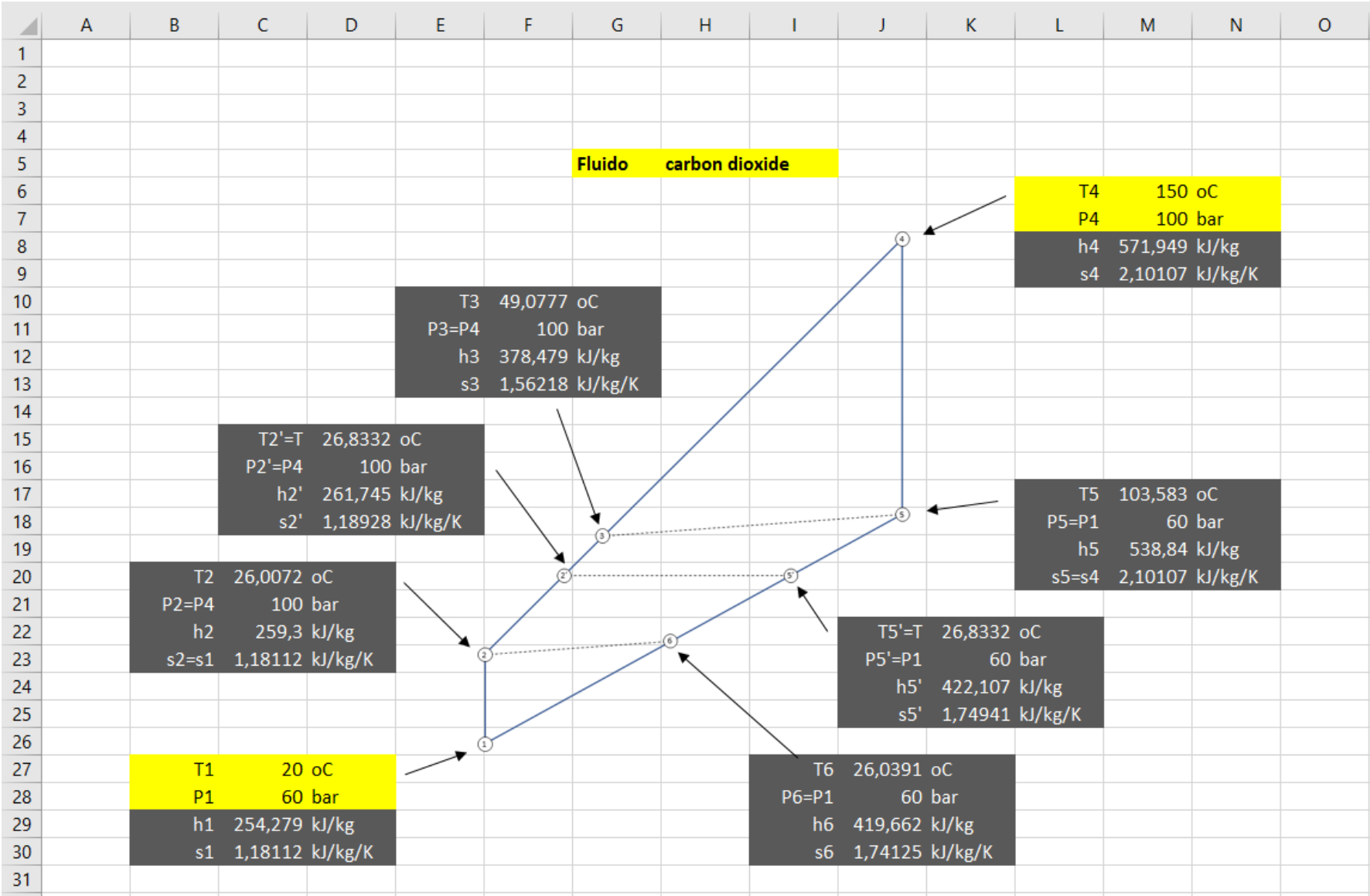
$$X_{n+1} = X_n - f_n / f'_n$$


P	Q	R	S	T	U
Tn	f(T)	f(T+eps)	f'(T)	Tn+1	erro
40	3,82392	3,82445	0,5295	32,7783	-7,2217
32,7783	1,37243	1,37266	0,22552	26,6927	-6,0856
26,6927	-0,0404	-0,0401	0,29048	26,8318	0,13906
26,8318	-0,0004	-0,0001	0,28457	26,8332	0,00145
26,8332	-1E-08	0,00028	0,28451	26,8332	4,7E-08
26,8332	8,9E-13	0,00028	0,28451	26,8332	-3E-12
26,8332	4,9E-15	0,00028	0,28451	26,8332	0
26,8332	4,9E-15	0,00028	0,28451	26,8332	0
26,8332	4,9E-15	0,00028	0,28451	26,8332	0

w12	-5,0216	kJ/kg
q23	119,178	kJ/kg
q34	193,471	kJ/kg
w45	33,1093	kJ/kg
q56	-119,18	kJ/kg
q61	-165,38	kJ/kg
imbal.	0	kJ/kg
recup.	0	kJ/kg
rend.1	0,14518	nd
rend.2	0,47255	nd
Carnot	0,30722	nd

$$\eta = \frac{(h_3 - h_4) - (h_2 - h_1)}{h_3 - h_2} = 8.98\%$$

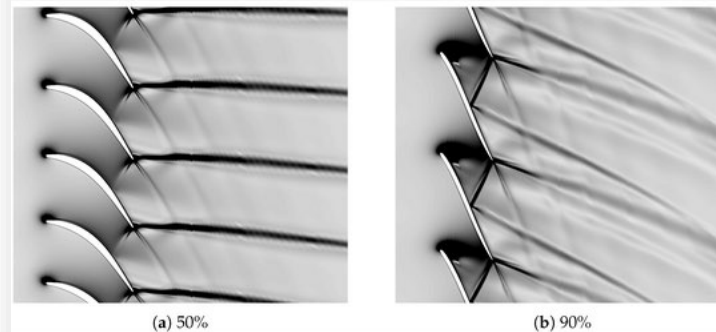
$$F(T_{\infty}) = C_P(100\text{bar} , T_{\infty}) - C_P(60\text{bar} , T_{\infty}) = 0$$



	ana. entrópica		
	$s_{gen,vc}$	0,106943 kJ/kg	$\frac{S_{gen,vc}}{m_B} = - \left( \frac{q_{34}}{T_H} + \frac{q_{61}}{T_L} \right)$
	$s_{gen,regen}$	0,021234 kJ/kg	$\frac{S_{gen,regen}}{m_B} = -s_5 - s_2 + s_3 + s_6$

→ Qual o significado físico destes valores ?

**Figure 3.** Steady solution (numerical Schlieren) in the rotor domain at 50% and 90% channel height.



- Transferência de calor  $\Delta T$  finito
- Atritos internos
- Compressão/expansão não resistida
- Mistura de substâncias diferentes
- Reações químicas espontâneas
- Onda de choque supersônico

# Curso de Termodinâmica

## TUTORIAL CICLOS parte 2/2



aula 15/20